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DECLINING INEQUALITY IN SCHOOLING IN BRAZIL
AND ITS EFFECTS ON INEQUALITY IN EARNINGS

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ABSTRACT

Household survey data demonstrate that Brazilian males born between 1925 and 1963 experienced steady increases in mean schooling and significant declines in schooling inequality. The variance in years of schooling increased for cohorts born up until 1950, with steady declines for more recent cohorts. Decomposition of a standard human capital earnings equation indicates that trends in schooling tended to reduce earnings inequality from 1976 to 1985, due to reductions in both the variance of schooling and in returns to schooling. These improvements were more than offset, however, by increases in other sources of inequality. Although the net increase in earnings inequality from 1976 to 1985 is disturbing, the reduction in schooling inequality represents a fundamental improvement in the determinants of earnings inequality in Brazil that will have beneficial effects for decades.

Key Words: Brazil, Inequality, Education, Income

Introduction

The relationship between the distribution of years of schooling in a population and the distribution of income has long been a fundamental issue in the literature on income inequality. Numerous studies have estimated the extent to which the distribution of schooling explains earnings inequality within and across populations, including studies directly linked to human capital models, such as Becker and Chiswick (1966) and Mincer (1974), and studies pursuing alternative theoretical interpretations, such as Jencks (1972) and Tinbergen (1972).

Research on developing countries has focused particular attention on the issue of how increases in the level of schooling over time affect earnings inequality. A number of authors (e.g. Chiswick, 1971, Knight and Sabot, 1987, and Marin and Psacharopoulos, 1976) have pointed out that the effect of educational expansion on earnings inequality is difficult to predict *a priori*, depending on specific changes in different levels of schooling, the relationship between schooling and earnings, and the change in that relationship as schooling increases. Several studies, such as Winegarden (1979), Ram (1984), and Tilak (1989), have attempted to clarify the relationship empirically by estimating cross-national regressions of the relationship between income inequality and measures of mean schooling and schooling inequality. These cross-national estimates provide conflicting empirical results, however, and for a variety of reasons give only a limited picture of the relationship between changes in the distribution of schooling and changes in the distribution of earnings over time.

The purpose of this paper is to take a detailed look at the changes in the distribution of schooling in recent decades in one developing country, Brazil, and to analyze the effects of those changes on the distribution of income. Brazil, with its high degree of income inequality and relatively low level of schooling in comparison to other countries with comparable levels of per capita income, is particularly appropriate for such a study. In the long debate over income inequality in Brazil, the role of education has frequently been emphasized, as in the well-known studies by Fishlow (1972) and Langoni (1973, 1977). Brazil's educational system is often criticized for producing both low levels of schooling and an unequal distribution of schooling in comparison to countries at similar income levels. There has been little systematic analysis, however, of changes in the distribution of schooling over time either in Brazil or in other developing countries.

This paper analyzes changes in the distribution of schooling for Brazilian males born between 1925 and 1963. We show that increases in mean schooling over this period were accompanied by steady decreases in inequality in schooling, as measured by the coefficient of variation and other mean-invariant measures. The variance of years of schooling, an important determinant of earnings inequality, increased along with the mean for cohorts born through the 1940's, but reached a peak among cohorts born around 1950 and has declined for more recent cohorts.

The relationship between these trends in the distribution of schooling and trends in earnings inequality are analyzed by decomposing a standard human capital earnings equation. The declining variance in years of schooling in and of itself implies a reduction in earnings inequality for more recent cohorts. The relationship is complicated, however, by changes in returns to schooling and by other sources of earnings inequality. Comparison of age and cohort profiles of inequality for 1976, 1982, and 1985 shows that earnings inequality in Brazil increased over this period. Based on our

decomposition we find that the contribution of schooling was to improve the distribution from 1976 to 1985, with declines in both the variance of schooling and in returns to schooling. Other sources of inequality increased, however, by a magnitude large enough to offset the beneficial changes in the distribution of schooling and in the relationship between schooling and earnings.

Changes in the Distribution of Schooling

We begin by documenting trends in the distribution of years of completed schooling for three-year birth cohorts of Brazilian males born between 1925 and 1963.¹ Our analysis is based on the 1985 *Pesquisa Nacional por Amostra de Domicílios* (PNAD), the annual household survey conducted by Brazil's census bureau, the *Instituto Brasileiro de Geografia e Estatística* (IBGE). We divide the sample into three-year age groups in order to follow trends in schooling over recent decades. Given the large sample size of the PNAD, analysis by three-year age groups allows us to have large sample sizes while maintaining relatively fine detail in cohort histories.² We use this nationally representative sample to infer the schooling histories of birth cohorts from 1925 to 1963. This will be appropriate if the sample truly represents the national population and if differential effects of mortality and emigration for different schooling groups are negligible for these cohorts.

Table 1 presents summary statistics describing the distribution of single years of completed schooling among three-year age groups in the 1985 PNAD.³ The steady increase in the mean level of completed schooling for Brazilian males can be seen in column 4 of Table 1 and in Figure 1. Although the level of schooling remains low, the mean years of completed schooling for Brazilian males has increased steadily over time, doubling over the four decades included here. Mean years of schooling rose from three years for the 1925-27 cohort to six years for the 1961-63 cohort. The most rapid increase in the mean occurred for the cohorts born from 1940 to 1954, most of whom attended school during the 1950's and early 1960's. The pace of the increase in the mean appears to have slowed beginning with the 1955-57 cohort, although incomplete schooling for the youngest cohorts may partially explain this leveling-off.

[Insert Figure 1 here.]

The variance in years of schooling for the same group of male cohorts is shown in Column 5 of Table 1. We will focus on the variance extensively below, since it will be shown to be a fundamental variable in our decomposition of earnings inequality. For expositional convenience we plot the standard deviation of years of schooling in Figure 1, since it is measured in units comparable to the mean. As the table and figure demonstrate, the standard deviation rises from

¹ Because we are interested in the distribution of income as well as schooling, we follow most of the literature on earnings and inequality by restricting our attention to males, avoiding the more difficult labor supply issues involved in analysis of female life cycle earnings.

² We have a sample of over 100,000 males in the cohorts being analyzed, with the smallest three-year age group containing over 2800 observations.

³ The results reported use the sample weights provided by IBGE to produce a representative sample of individuals for the Brazilian population. Sample sizes reported refer to the unweighted number of observations. All statistics are calculated using the sample weights. The algorithm used to construct the variable for single years of schooling is available from the authors on request.

**Table 1. Years of Completed Schooling for Three-Year Age Groups
Brazilian Males, 1985 PNAD**

Age Group	Birth Cohort	Sample Size	Mean	Variance	Coeff. of Variation	Percent Completing			
						0 Years	4+ Years	8+ Years	11+ Years
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)
22-24	1961-63	13937	5.98	16.08	0.67	11.8	72.2	37.8	20.0
25-27	1958-60	13024	5.93	17.80	0.71	12.2	70.9	36.4	20.9
28-30	1955-57	11734	5.89	19.33	0.75	13.2	70.2	34.9	21.8
31-33	1952-54	10622	5.77	20.66	0.79	14.2	67.0	32.9	21.6
34-36	1949-51	9643	5.24	21.00	0.87	17.9	61.3	28.4	18.8
37-39	1946-48	8386	4.95	20.84	0.92	19.1	57.8	25.4	16.9
40-42	1943-45	7634	4.43	19.12	0.99	23.4	52.5	21.6	14.3
43-45	1940-42	7123	4.08	17.79	1.03	25.2	48.2	18.9	12.5
46-48	1937-39	6109	3.92	16.75	1.04	26.5	47.6	17.7	11.3
49-51	1934-36	5588	3.78	16.52	1.08	28.2	46.1	16.7	10.8
52-54	1931-33	4942	3.58	15.70	1.11	30.7	44.3	15.5	10.0
55-57	1928-30	4590	3.32	14.84	1.16	33.7	40.9	13.9	8.6
58-60	1925-27	4099	3.05	14.03	1.23	37.3	37.7	12.3	7.7
22-60	1925-63	107431	4.98	19.11	0.88	19.6	59.3	27.2	16.8

the 1925-27 cohort to the 1949-51 cohort, then declines for cohorts born in the 1950's and 1960's. This peak in the variance in years of schooling was previously noted in Lam and Levison (1990), using data from the 1976 PNAD. It is more firmly established here using the 1985 data, since the 1949-51 cohort was 34-36 years of age at the time of the 1985 survey, old enough that acquisition of schooling should have been virtually complete.⁴ The peak in the variance of schooling will be a permanent characteristic of the distribution of schooling during the lifetime of the 1949-51 cohort, and has important implications for the distribution of earnings.

Figure 1 also demonstrates an important feature of the change in mean-adjusted schooling inequality. Although the standard deviation in years of schooling increased over time for cohorts born between 1925 and 1948, it never increased as fast as the mean, as it would have if there had been proportional increases in schooling throughout the population. This implies that the coefficient of variation, a standard inequality measure that is independent of the mean, declined steadily during the four decades under consideration. The coefficient of variation (the standard deviation divided by the mean) is shown in column 6 of Table 1. By this measure, inequality in schooling for Brazilian males has declined steadily in recent decades. While mean schooling has doubled, the coefficient of variation has been almost cut in half.⁵

⁴ If schooling is incomplete for the younger cohorts, the variance in years of schooling will be understated for those cohorts. Comparison of the same cohorts in other years suggests that the peak in the variance of schooling is not simply an artifact of this effect, as will be discussed further below.

⁵ Lam and Sedlacek (1990), using the same data, document a similar pattern for Brazilian women. Mean schooling for women rose from 2.7 years for the 1925-27 cohort, eventually surpassing males to reach a level of 6.3 years for the 1961-63 cohort. Females exhibit a peak in the variance of schooling with the 1952-54 cohort, slightly later than that for men.

This pattern of a rising mean and falling coefficient of variation is not unique to Brazil. Psacharopoulos and Arriagada (1986) present estimates of the proportion of the labor force with various levels of schooling, along with an estimate of mean schooling, for a large number of countries. Data are reported for more than one year for twenty countries. Ram (1990) uses the grouped data to estimate the standard deviation for each population. Although these numbers are only roughly comparable to ours, since they apply to the entire labor force rather than to specific cohorts, and since they are based on categorical frequency distributions rather than the single-year of schooling data we use, it is possible to compare changes over ten to twenty year intervals in means, standard deviations, and coefficients of variation. Among these twenty countries, Brazil has one of the largest increases in mean schooling, both absolutely and proportionately, with somewhat slower growth than that of Korea, but faster growth than most other Asian countries and most Latin American countries. In all twenty countries mean schooling rose at a faster rate than the standard deviation, implying reductions in mean-adjusted inequality in schooling in all cases.⁶

One important component of the rising mean in the years of schooling in Brazil is the falling proportion with zero years of completed schooling, shown in column 7 of Table 1. The percentage of males with no schooling has declined steadily, falling from 37 percent for the 1925-27 cohort to under 12 percent for the 1961-63 cohort. Columns 8, 9, and 10 of Table 1 show other important points in the cumulative distribution. The proportion with at least four years has increased from 38 percent to 73 percent, the proportion with at least eight years (completion of primary school) has increased from 12 percent to 38 percent, and the proportion with at least eleven years (completion of high school), has increased from 8 percent to 20 percent. The fact that the proportion with high school education appears to have declined for the most recent cohorts suggests that incomplete schooling may complicate results for the younger cohorts, an issue discussed further below.

A more complete picture of the changes in the distribution of schooling is provided by comparing the single year frequency distributions for three particular cohorts: 1925-27, the oldest cohort in Table 1; 1949-51, the cohort with the highest variance in schooling; and 1961-63, the youngest cohort in Table 1. Figure 2 plots the frequency distribution of years of schooling for these three cohorts. The basic shapes of these densities are quite similar, with peaks at zero, four, eight, and eleven years, consistent with completion of levels of the Brazilian schooling system. The most striking difference between the oldest and youngest cohorts is the sharp decline in the proportion with zero schooling. The proportion earning exactly four years is remarkably constant across the three cohorts. This should not be interpreted as indicating inertia in the distribution of schooling, however. Figure 2 demonstrates that all levels of schooling under four years have become less

⁶ Ram (1990) uses the standard deviation as his measure of schooling inequality, rejecting mean-adjusted measures such as the coefficient of variation because, among other reasons, they do not equal zero when the mean is zero. Ram's criterion is an odd one, since most inequality measures satisfying standard axioms will violate it. We use the variance of schooling in our decompositions of earnings inequality below, but follow the conventional literature on income inequality by maintaining the conceptual distinction between changes in means and changes in mean-adjusted dispersion, using the term "inequality" to refer to measures that are independent of the mean. We also follow previous literature on schooling inequality, such as the classic study by Jencks (1972), who uses the coefficient of variation as a measure of schooling inequality.

prevalent over time, while levels of schooling over four years have become more prevalent, with four years being roughly the point at which the densities intersect.

[Insert Figure 2 here.]

The cumulative schooling distributions implied by the densities in Figure 2, and shown in the last four columns of Table 1, come very close to indicating first order stochastic dominance in the distributions over time, the condition that would be implied if the cumulative distributions did not intersect. An instructive way to interpret these distributions is to imagine utility defined as a function of years of schooling: $U(S)$. Given a utilitarian social welfare function $\int U(S)f(S)dS$, first order stochastic dominance implies higher social welfare for *any* function $U(S)$ that is increasing in S . Thus, first order stochastic dominance would imply that the distribution of schooling in Brazil has unambiguously improved over time. It is even stronger than second order stochastic dominance, which would imply higher social welfare for any *concave* function $U(S)$ (see Atkinson, 1970; Kakwani, 1980; Shorrocks, 1983; and Lam, 1988). As can be seen from the last four columns of Table 1, there is close to unambiguous improvement in the schooling distributions by the criterion of first order stochastic dominance for every cohort in comparison to the cohorts preceding it.

The cumulative distributions imply unambiguous improvements in the distribution of schooling across cohorts of Brazilian males, using the same criteria of stochastic dominance used for comparing non-mean-adjusted income distributions (Shorrocks, 1983). Much of this improvement results from increases in the mean. In comparing income distributions, it is standard practice to also consider mean-adjusted measures of dispersion which abstract from the mean level of income. In the same spirit, it is instructive to consider whether inequality in schooling, abstracting from the mean, has declined over time in Brazil. We have already seen that one standard inequality measure, the coefficient of variation, does in fact decline steadily over the period we consider. A more complete comparison can be made by analyzing Lorenz curves for the distribution of schooling, defined — analogously to Lorenz curves for income — as the cumulative proportion of years of schooling plotted against the cumulative proportion of the population.

Figure 3 shows Lorenz curves for years of schooling for the same three cohorts analyzed above. The figure shows that the Lorenz curve for schooling shifts unambiguously upward over time, implying unambiguous improvements in schooling equality. For example, the least educated fifty percent of the population in the 1925–27 birth cohort had less than eight percent of the total years of schooling of that cohort. For the 1961–63 birth cohort, the least educated fifty percent had 23 percent of the total years of schooling. The Lorenz curves indicate that the share of years of schooling accounted for by those at the bottom of the distribution has risen steadily over time.

[Insert Figure 3 here.]

Analysis of Lorenz curves for the distribution of schooling is unusual, but it follows naturally from any analysis of schooling inequality.⁷ To interpret these Lorenz curves, consider the relationship between Lorenz curves for the distribution of schooling and Lorenz curves for the distribution

⁷ Jencks (1972), in fact, presents what amount to points on Lorenz curves for schooling across birth cohorts in his classic study of schooling inequality and earnings inequality in the United States.

of income. From the literature on Lorenz curves and social welfare we know that Lorenz dominance in income implies higher social welfare for any concave utility function, abstracting from changes in the mean (Atkinson, 1970; Shorrocks, 1983). Mapping from schooling to utility through income, $U[Y(S)]$, Lorenz dominance in schooling implies unambiguously higher social welfare, even with no increase in mean schooling, if utility is a concave function of schooling. Sufficient (but not necessary) conditions for utility to be a concave function of schooling are (i.) that income is a concave function of schooling and (ii.) that utility is a concave function of income. While these conditions sound plausible at first, it is noteworthy that income is actually a *convex* function of income in the most standard representation, the conventional log-linear human capital earnings equation: $\ln Y = \alpha + \beta S$. An implication of this functional relationship is that we may observe an unambiguously more equal distribution of schooling, as indicated by Lorenz dominance in schooling distributions, accompanied by an unambiguously *less* equal distribution of earnings, as indicated by Lorenz curves for earnings, even if schooling completely determines earnings. It will be seen below that the unambiguous improvements in mean-adjusted inequality in schooling in Brazil did not necessarily imply improvements in the distribution of earnings in Brazil during the period in which the variance in years of schooling was increasing.

Implications for the Distribution of Income

The changes in the distribution of schooling documented above could be expected to have important implications for the distribution of earnings. The link between schooling and the distribution of income has been emphasized in the literature on income inequality. Predictions based on a human capital model were made by Becker and Chiswick (1966) and Chiswick (1971), including a prediction that decreasing inequality in schooling would lead to decreasing inequality in earnings. Empirical tests based on cross-national data provide mixed evidence.⁸ Winegarden (1979) found mean schooling negatively associated with income inequality, and the variance of schooling positively associated with income inequality based on data for 32 countries. Ram (1984) found only marginally significant effects based on data for 28 countries, with the variance of schooling having an equalizing, rather than disequalizing, effect. As emphasized by Knight and Sabot (1987), rising mean levels of education can in principle either increase or decrease earnings inequality, depending on the specific changes in different levels of schooling and on the relationship between schooling and earnings. As we will see below in the case of a human capital earnings equation, it is possible to generate decreases in inequality in schooling simultaneously with *increases* in inequality in earnings.

One natural way to link the distribution of schooling to the distribution of earnings is in the context of a simple conventional earnings equation

$$\ln Y_i = \alpha + \beta S_i + u_i, \quad (1)$$

where $\ln Y_i$ is the natural logarithm of the i th individual's labor earnings, S_i is the i th individual's years of schooling, and u_i is a residual representing all other determinants of the i th individual's

⁸ See Tilak (1989) for a recent survey of this literature.

earnings. We omit experience from the earnings equation, since for narrow age groups a standard experience proxy will be almost perfectly correlated with years of schooling. Equation (1) can be thought of simply as an empirically appropriate functional form or can be motivated by a human capital model of earnings, as in Mincer (1974). Whatever the motivation, specifying equation (1) in the conventional semi-log form means that it provides an analytically simple decomposition of the variance of log earnings, a standard measure of inequality.⁹

Assuming that α and β represent constants across the population, the variance of log earnings $V(\ln Y)$ implied by equation (1) is

$$V(\ln Y) = \beta^2 V(S) + V(u) + 2\beta C(S, u), \quad (2)$$

where $V(S)$ is the variance in years of schooling, $V(u)$ is the variance in components of earnings uncorrelated with schooling, and $C(S, u)$ is the covariance between schooling and variables omitted from the earnings equation.

According to equation (2), the variance of years of schooling is a fundamental determinant of the variance in log earnings. If schooling is uncorrelated with other determinants of earnings not included in the simple earnings equation (1), then changes in the variance of schooling lead directly to changes in earnings inequality by a factor that is the square of returns to schooling. If returns to schooling are constant and "residual variance" is constant, then earnings inequality, as measured by the log variance, is simply a linear function of the variance in years of schooling.

Equation (2) implies that it is possible for earnings inequality to increase at the same time that schooling inequality is declining. According to the equation, inequality in earnings is a function only of the *variance* in years of schooling, with no independent effect of mean schooling. But inequality in schooling, as conventionally defined, is a function of both the variance and the mean. If the variance in schooling rises while the coefficient of variation in schooling falls, then we will observe an increase in earnings inequality at the same time as a *decrease* in schooling inequality. This is exactly the situation that applies to cohorts of Brazilian males born between 1925 and 1951. Although successive cohorts had declining inequality in schooling by all mean adjusted measures of inequality, we would expect them to have increasing earnings inequality because of the increase in the variance in schooling over this period. For cohorts born after 1951 both mean-adjusted inequality in schooling and the variance in schooling declined, implying declining inequality in earnings.

We will use equation (1) as the basis for analyzing the relationship between the distribution of schooling and the distribution of earnings. We will adopt a human capital interpretation of equation (1), but recognize that the estimate of β may capture effects other than strictly private returns to schooling. Correlations between schooling and omitted variables will not only affect

⁹ In addition to the fact that use of the variance in log earnings follows naturally from the human capital earnings equation, it is a widely used inequality measure. It satisfies most standard axioms for inequality measures and among the class of conventional measures gives relatively more weight to the bottom of the distribution (see Kakwani, 1980, and Atkinson, 1970).

interpretation of the coefficient on schooling, but imply that the final term in equation (2) cannot be ignored in decomposing the variance of log earnings. Changes in the distribution of schooling may in such a case affect the variance in log earnings not only through the "explained variance," $\beta^2 V(S)$, but also through "unexplained variance."

Although our primary interest is not in estimates of returns to schooling *per se*, the appropriateness of the specification of earnings equation (1) does affect the interpretation of our results. If returns to schooling are nonlinear, for example, then the variance in log earnings will depend on higher moments of the schooling distribution beyond the variance. If a quadratic term belongs in the earnings equation, then it is not precisely accurate to interpret the "explained variance" from estimation of equation (1) as capturing all effects of the distribution of schooling. While the explained variance captures all effects on income that are correlated with schooling, it will not capture higher order effects that would show up, for example, as correlations between income and schooling squared. We use the specification in equation (2) because it provides an analytically simple decomposition of age-specific inequality. The addition of simply a quadratic schooling term, for example, would add two additional components to the decomposition, one depending on the kurtosis of the schooling distribution, and one depending on the skewness. While such a decomposition might be instructive, we believe the linear decomposition captures the most important components of the relationship between schooling inequality and earnings inequality.¹⁰

An additional assumption implicit in our interpretation of the decomposition in equation (2) is that there are constant returns to schooling within any cohort. We thus omit one of the determinants of earnings inequality in the theoretical decomposition of Becker and Chiswick (1966) and Chiswick (1971), the variance in returns to schooling. Given variance in *returns* to schooling, a rising mean level of schooling will tend to increase earnings inequality even if the variance in *years* of schooling is constant. Our results should also be qualified by well-known warnings that the coefficient on schooling includes the effects of many omitted variables correlated with schooling. It is often argued that in Brazil, as in many developing countries, high levels of schooling are more concentrated among the children of wealthy families than they are in the U.S., so that schooling may partly serve as a proxy for status and family connections. Identifying the precise meaning of the strong association between schooling and earnings in Brazil is beyond the scope of this paper, but we note that caution should be used in applying a strict human capital interpretation to the results.¹¹

Earnings Equations and the Decomposition of Earnings Inequality, 1985

In order to analyze the relationship between the distribution of schooling and the distribution of earnings for the cohorts discussed above we present estimates of earnings equation (1) for separate

¹⁰ As will be demonstrated below in discussing the robustness of our results, the simple linear specification is in fact a surprisingly good fit for the separate three-year age groups we use for our regressions.

¹¹ We also recognize that we are abstracting from many historical and institutional determinants of inequality, particularly in regard to the large regional variations in inequality in Brazil. We have repeated our analysis for separate regions of Brazil and for rural and urban samples. These results are reported in Lam and Levison (1989) and are summarized briefly below.

Table 2. Monthly Labor Earnings by Years of Age
Descriptive Statistics and Age-Specific Earnings Equations
Brazilian Males with Positive Earnings, 1985 PNAD

Age Group	Birth Cohort	Sample Size	Mean Earnings (x.001)	Mean Log Earnings	Variance Log Earnings	Age-Specific Earnings Equation				
						$\hat{\beta}$	Std.Err.	R^2	$V(u)$	$\hat{\beta}^2 V(S)$
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)
22-24	1961-63	11689	801	13.25	0.638	0.110	0.0016	0.296	0.449	0.189
25-27	1958-60	11763	1080	13.48	0.773	0.126	0.0015	0.366	0.490	0.283
28-30	1955-57	10956	1330	13.65	0.865	0.135	0.0016	0.406	0.514	0.352
31-33	1952-54	10022	1572	13.75	0.987	0.147	0.0016	0.455	0.538	0.449
34-36	1949-51	9152	1666	13.76	1.066	0.155	0.0017	0.478	0.556	0.509
37-39	1946-48	7919	1781	13.78	1.126	0.158	0.0019	0.469	0.598	0.528
40-42	1943-45	7157	1708	13.75	1.103	0.163	0.0021	0.469	0.585	0.518
43-45	1940-42	6565	1639	13.70	1.095	0.164	0.0023	0.445	0.608	0.487
46-48	1937-39	5497	1664	13.67	1.114	0.164	0.0026	0.416	0.651	0.463
49-51	1934-36	4788	1584	13.64	1.122	0.164	0.0029	0.401	0.673	0.450
52-54	1931-33	3982	1542	13.59	1.097	0.165	0.0033	0.388	0.672	0.425
55-57	1928-30	3463	1352	13.47	1.107	0.160	0.0038	0.343	0.727	0.380
58-60	1925-27	2841	1334	13.38	1.156	0.171	0.0045	0.341	0.762	0.394
22-60	1925-63	95794	1424	13.61	0.998	0.138	0.0006	0.370	0.629	0.370

Note: "Earnings" refers to total earnings in cruzeiros from all jobs in the month prior to the survey (September 1985). Figures for mean earnings in column 4 are divided by 1000. Regression results are for OLS regression $\ln Y_i = \alpha + \beta S_i$ for each age group.

three-year age groups of Brazilian males with positive monthly earnings in the 1985 PNAD. These regressions, along with descriptive statistics for earnings, are presented in Table 2.¹²

For graphical analysis of the results in Table 2 we can use either year of birth or age as the unit of reference. While the choice is at one level simply a question of whether to read the table from top to bottom or bottom to top, it draws attention to more fundamental conceptual issues in analyzing earnings inequality across age groups. The mean and standard deviation of schooling, plotted in Figure 1 as a function of year of birth, could appropriately be thought of as properties of cohorts. That is, they vary by age for adults in a single cross-section because of changes in schooling over time, not because of a fundamental relationship between schooling and age. Labor earnings, on the other hand, vary systematically with age, and could be thought of as a function of age rather than cohort. We graph the components of earnings as a function of age in the following figures, recognizing that what we see is a combination of "age" and "cohort" effects, with the relative importance of the two components varying from graph to graph.

Figure 4 shows the variance in log earnings for each age group, along with the explained and unexplained components of this variance implied by our estimates of equation (1) for each age group.

¹² Changing from the sample of all Brazilian males to the sample of Brazilian males with positive labor earnings causes some changes in the distribution of schooling. The differences in the two samples depend on the age group. At younger ages the sample of working males has slightly higher mean schooling than all males, while at older ages the sample of working males is slightly less educated than the sample of all males. The differences are modest, however, and do not cause any significant changes in the patterns of mean and variance of schooling across cohorts documented above.

The shape of the age profile of inequality has important implications for the relationship between the age composition of the population and the overall distribution of income.¹³ As shown in Figure 4 and in Column 6 of Table 2, the variance of log earnings for Brazilian males rises steeply from age group 22–24 to age group 37–39, then is relatively flat for older ages. The relationship between age and inequality shown in Figure 4 is similar to the pattern estimated by Langoni (1973) for separate age groups of Brazilian males using the 1970 census. The pattern differs significantly from the relationship between age and earnings inequality in the United States: Mincer (1974), Schultz (1975), and Smith and Welch (1979) all find U-shaped profiles of inequality by age in cross-section estimates for U.S. males.¹⁴ As discussed in more detail in Lam and Levison (1990), the shape of this age profile of inequality is a result of interactions between the cohort profile of variance in schooling, changes in returns to schooling by age, and the age profile of residual variance.

The increase in inequality from age group 22–24 to age group 37–39 in Figure 4 is consistent with our predictions based on the cohort profile of the variance in schooling documented above. The increase in inequality with age suggests that the declining variance in schooling across cohorts is causing the decline in inequality in earnings for more recent cohorts. The explanation for the age profile of inequality is in fact more complicated, however. As we will see below, changes in the variance of schooling across cohorts are only one part of the explanation for the relationship between age and inequality in Brazil.

[Insert Figure 4 here.]

Returning to equation (2), we note that an important determinant of the variance in log earnings is the returns to schooling.¹⁵ Column 7 of Table 2 indicates that estimated returns to schooling vary significantly as a function of age in Brazil, rising steeply from age group 22–24 to age group 40–42, then remaining relatively flat at higher ages.¹⁶ Both age and cohort factors may play a role in determining this profile. Knight and Sabot (1981), for example, suggest that higher levels of schooling for younger cohorts may explain the frequently observed increase in returns to schooling with age. Comparisons with estimates from the 1976 and 1982 PNADs, presented below, reveal a very similarly shaped age profile, however, suggesting that there is some persistent systematic relationship between age and returns to schooling in Brazil.

Returns to schooling combine with the variance in years of schooling to account for the “explained variance” in earnings inequality, $\beta^2 V(S)$, in equation (2). Column 10 of Table 2 and Figure 4 show this explained variance from the earnings regressions for three-year age groups. The ex-

¹³ See, for example, Paglin (1975), Morley (1981) and Lam (1984).

¹⁴ The profile of earnings inequality by *experience* has also been estimated by a number of researchers. See Lam and Levison (1990) for a discussion of this literature and comparisons of age and experience profiles of inequality in Brazil and the U.S.

¹⁵ Overall, estimated returns to schooling for males aged 22–60 are 0.138 in 1985. This is close to Senna’s (1976) estimates of 0.125 and 0.127 for Brazilian males, using the same simple earnings function and a 1970 Ministry of Labor survey.

¹⁶ Standard errors are consistently very small, and the estimates of returns to schooling are, without exception, significant at the one percent level.

plained variance is highest for men ages 37–39, representing cohorts born in 1946–48. The two elements of this explained variance behave very differently in the degree to which they are “age” or “cohort” driven. The variance of schooling is primarily a characteristic of cohorts, remaining constant once a cohort is beyond about age 25. As shown above, the variance of schooling is highest for the 1949–51 cohort, corresponding to the 34–36 age group in 1985. Theoretical arguments could be made for both age and cohort effects in returns to schooling, especially in a population experiencing rapid changes in the level of schooling. Whatever the explanation for the age pattern in returns to schooling, it interacts with the cohort pattern in variance of schooling to produce the relationship between age and “explained variance” shown in Figure 4.

The residual (unexplained) variance in the age-specific earnings equations is shown in column 9 of Table 2 and in Figure 4. Residual variance rises fairly steadily from age 19–21, increasing from .45 for the youngest cohort to .76 for the oldest cohort. This residual variance includes variance resulting from post-schooling investments in human capital, such as on-the-job training and experience, as emphasized by Mincer (1974). It may also pick up effects of changes in schooling to the extent that schooling is correlated with variables omitted from the simple log-linear earnings equation (1). In any case, from an accounting perspective, it is an important explanation of the fact that inequality increases with age for Brazilian males.

Changes in Earnings Inequality, 1976–1982–1985

Have the improvements in the distribution of schooling in Brazil documented above led to improvements in the distribution of earnings? In this section we compare the earnings distributions for 1976, 1982, and 1985 in order to document the changes in earnings inequality over this period and to identify the role of schooling in those changes.¹⁷ In comparing income distributions across periods, a fundamental problem of identification exists. If we compare the same age group in different periods, different cohorts are being compared. If we compare the same cohort in different periods, we are capturing the cohort at different points in the life cycle. Thus, cohort effects will appear to be period effects when we control for age, and age effects will appear to be period effects when we control for cohort. Figures 5 and 6 demonstrate the problem in comparing income distributions across time in Brazil.

[Insert Figure 5 here.]

Figure 5 shows the variance in log earnings for three-year age groups of Brazilian males using the 1976, 1982, and 1985 PNADs. The figure shows that inequality is higher for every age group in 1985 than in 1982, and is higher in 1985 than in 1976 for all age groups above 34. Figure 6 plots the same data as a function of birth cohort rather than age.¹⁸ Every birth cohort has higher earnings inequality in 1985 than in 1982 and 1976. Every birth cohort except that of 1925–27 has higher earnings inequality in 1982 than in 1976.

¹⁷ In making this comparison we are assuming that the PNAD surveys for these three years are consistently representative of the national population. The validity of this assumption is discussed below.

¹⁸ The cohort figures include only the observations for age groups greater than 21 years of age.

[Insert Figure 6 here.]

In spite of the impressive improvements in the distribution of schooling, the fact that earnings inequality increased for every birth cohort and most age groups from 1976 to 1985 shows that the distribution of earnings was worsening. What is the explanation for this disturbing increase in inequality, and how do we reconcile it with the improvements in the distribution of schooling? Once again, a decomposition of earnings inequality is instructive.

Changes in the Distribution of Schooling

Looking first at Figure 5, what is the explanation for the increase in inequality for every age group from 1982 to 1985 and for older age groups from 1976 to 1985? An important part of the explanation is a cohort effect for older age groups resulting from the changing distribution of schooling over time. This cohort effect is completely independent of changing economic conditions, and thus should not be attributed to differences in the Brazilian economy in 1976, 1982, and 1985. An instructive example is provided by the 37–39 year age group in Figure 5, an age group which shows large changes in inequality across the three periods. This age group corresponds to the 1946–48 birth cohort in 1985, the 1943–45 birth cohort in 1982, and the 1937–39 birth cohort in 1976. Looking back at Table 1, we see that these three cohorts had very different variances in years of schooling. The large differences in earnings inequality for this age group in the three periods are primarily attributable to the changes in the variance of schooling over time, without necessarily implying anything about the economic conditions of the three periods.

We thus see how the changes in the distribution of schooling in Brazil can affect the distribution of income over time. In the case of the three survey years being compared here, this cohort effect is disqualifying for older age groups and equalizing for younger ones. For older ages, the birth cohort at a given age in 1985 had a higher variance of schooling than the birth cohort at that same age in 1982. This is true for cohorts born before the peak in the variance in schooling. For younger ages, the birth cohort at a given age in 1985 should have had a *lower* variance of schooling than the birth cohort at that age in 1982.

The problem of potentially misleading cohort effects shown in Figure 5 can be avoided by comparing *cohorts* over time rather than *age groups*. Figure 6 compares earnings inequality in 1976, 1982, and 1985 for the same birth cohorts. Since the variance of schooling should remain constant for a cohort over time, the increases in inequality for birth cohorts shown in Figure 6 cannot be attributed to changes in the variance of schooling. The comparisons across cohorts in Figure 5 introduce another source of potentially misleading inference, however. The changes in earnings inequality over time for a given birth cohort will be affected by changes in either returns to schooling or residual variance as a function of age. From the results presented above we know that both returns to schooling and residual variance vary significantly with age in Brazil. We therefore look at each of these variables for 1976, 1982, and 1985 to investigate their possible role in explaining the increase in earnings inequality in Brazil during this period.

Changes in Returns to Schooling

As emphasized above, one of the critical factors affecting changes in inequality across periods is changes in returns to schooling. Langoni (1973) emphasized the role of changes in returns to

schooling in explaining apparent increases in inequality in Brazil during the 1960's and 1970's. Langoni argued that inequality increased in that period partly because of an increase in returns to schooling, a result of quasi-rents to human capital caused by Brazil's rapid (and presumably unexpected) economic growth.

Figure 7 shows returns to schooling for each three-year age group in 1976, 1982, and 1985, based on estimates of earnings equations of the form of equation (1). The figure shows that returns to schooling fell over time for every age group, a decline which in and of itself should imply a decline in earnings inequality for every age group over the period. In the case of older age groups, the decline in returns to schooling tends to offset the increase in inequality resulting from the fact that cohorts with higher variance in schooling moved into those age groups in 1985. For younger age groups the decline in returns to schooling reinforces the decrease in inequality resulting from the fact that cohorts with *lower* variance in schooling moved into those age groups in 1985.

[Insert Figure 7 here.]

The decline in returns to schooling at every age group in Brazil during this period is noteworthy, although we cannot be certain if it represents long-term trends or short-run period effects. Trends in the overall level of returns to schooling will be an important determinant of long-term trends in earnings inequality in Brazil. Like many other developing countries, Brazil has typically had much higher estimated returns to schooling than the United States and other industrialized economies (see Psacharopoulos, 1981, and Schultz, 1988). Lam and Levison (1990), for example, find that the estimated returns to schooling for Brazilian males are higher by around five percentage points than returns to schooling for males in the United States for almost every age group.

The decline in returns to schooling in Brazil for every age group between 1976 and 1985 may indicate that the increasing mean level of schooling in Brazil is leading to a dissipation of high rents to what has in the past been relatively scarce human capital. If this is true it implies that earnings inequality should diminish over time as increasingly better educated birth cohorts enter the labor force. Whether the decline in returns to schooling shown in Figure 7 is a permanent trend or a result of short-run cyclical conditions in the Brazilian economy in the three years shown¹⁹, it remains true that this decline had an *equalizing* effect over this period.

Residual Variance

Since our estimates indicate that there was both a decrease in the variance of schooling and a decrease in the returns to schooling over the period 1976 to 1985, the overall increase in inequality between 1976 and 1985 shown in Figure 5 and Figure 6 is not attributable to schooling, at least in the accounting implied by the decomposition of equation (2). The contribution of schooling to inequality over this period was to improve the distribution of income. It follows that changes in residual variance, the variance in the components of earnings uncorrelated with schooling, must play an important role. Appendix Table A details the elements of the inequality decomposition for 1976 and 1982, paralleling Table 2's breakdown for 1985. A comparison of residual variance for

¹⁹ In 1976 economic conditions were declining after the boom years of 1968-74; the recession bottomed out in 1982-83, and conditions were on the upswing in 1985.

age groups and birth cohorts, based on the estimation of earnings equation (2) for 1976, 1982, and 1985, shows that residual variance is higher for every age group and for every birth cohort in 1985 than in 1982 and 1976. Changes in residual variance from 1976 to 1982 are less clear. Although there is a small increase in inequality for most birth cohorts from 1976 to 1982, this is primarily the result of the strong tendency for residual variance to increase with age in Brazil. In fact, every age group but one had lower residual variance in 1982 than in 1976.

The overall increase in residual variance from 1976 to 1985 for both age groups and birth cohorts is large enough to overcome the equalizing effects of declining variance in years of schooling and declining returns to schooling. This is disturbing, since it implies that Brazil failed to experience the improvements in the distribution of income that should have resulted from changes in the distribution of schooling and the returns to schooling. On the other hand, to the extent that residual variance as we measure it (i.e. the variance in the components of earnings that are uncorrelated with schooling) is being driven by short-term cyclical effects, including perhaps the rate of inflation, it may be reassuring that the increase in inequality from 1976 to 1985 can be attributed to residual variance. The equalizing effects of the improved distribution of schooling represent a fundamental change in the determinants of earnings inequality in Brazil. This schooling component of inequality will persist for decades in Brazil. The fact that succeeding cohorts of Brazilian males have continually lower variance in years of schooling will in and of itself improve the distribution of earnings in the future. As the cohorts who experienced the highest variance in schooling, those born around 1950, move through the age distribution and are replaced by more recent cohorts, overall inequality in Brazil should begin to demonstrate the kind of improvements that can now only be seen by looking at narrow age groups.

Robustness of the Results

The results presented above are potentially sensitive to a number of assumptions. If the 1985 PNAD survey does not accurately represent the national population of Brazil, then cohort-type analysis based on this cross-section will be misleading, affecting our conclusions about changes in the distribution of schooling over time. If some men in younger cohorts have not completed schooling at the time of the 1985 survey, the observed decline in the variance of schooling may be an artifact of incomplete schooling. If the 1976, 1982, and 1985 PNAD surveys are not consistent with each other, then our conclusions about changes in returns to schooling over time may be unreliable. Misspecification of the earnings equation is another concern, since it could affect the validity of the returns to schooling estimates and the interpretation of our decomposition. In this section, we provide a brief examination of these issues.

Comparison of the schooling distribution for the same cohorts across different sample years provides evidence on both the consistency of the PNAD samples and on the potential effects of incomplete schooling for younger men. The 1976, 1982, and 1985 samples provide quite consistent estimates of mean schooling across cohorts once cohorts reach their mid-thirties. Discrepancies between mean schooling for the same cohorts in 1982 and 1985 are typically less than one-tenth of a year, a quantity that is one-third to one-half as large as the change in mean schooling from one three-year age group to the next. The 1976 sample is somewhat less consistent, with means on the

order of 0.3 to 0.4 years below those of 1985 for almost all cohorts. Comparisons of the variance in schooling suggest that incomplete schooling does contribute to falling variances for younger cohorts. The observed peak in variance appears to be real, however. The 1946–48 cohort has the highest schooling variance in both the 1976 and 1982 samples, changing to the flat peak across the 1946–48 and 1949–51 cohorts in the 1985 sample, documented in Figure 1. We conclude from our comparisons that the 1982 and 1985 samples are highly consistent, suggesting that the assumption that they provide a consistent sample of the national Brazilian population is reasonable. We are somewhat less confident of the comparability with the 1976 survey, although it provides a very similar picture of the basic patterns in both the mean and variance of schooling. It appears clear that there has been at least a substantial flattening of the variance in years of schooling across cohorts, with fairly compelling evidence that the variance has been declining for cohorts born since the early fifties.

In order to test the robustness of our assumption of a linear specification of the earnings equation, we used the 1985 data to estimate more flexible specifications. Our sample sizes are large enough for most age groups to allow us to estimate regressions using eighteen dummy variables for the individual years of schooling. In addition to testing the robustness of our linearity assumption, these estimates are interesting in their own right for the picture they provide of the relationship between schooling and earnings in Brazil. Figure 8 shows the results for three representative age groups. The coefficients show log earnings for each schooling level relative to men with zero schooling. Given small cell sizes in some single year schooling categories, these non-parametric estimates for different age groups are surprisingly regular, and suggest a remarkably linear relationship between log earnings and schooling. As evidence of the reasonableness of the linear specification, we compared the R^2 for earnings regressions using a linear specification, a quadratic specification, and the non-parametric specification with 18 dummies. For the 34–36 year old age group, for example, these R^2 s are .478, .479, and .488 respectively. Similar modest improvements in explanatory power by moving to a more flexible functional form are observed for all age groups.²⁰

[Insert Figure 8 here.]

As a final test of the sensitivity of our results we considered regional variations in the patterns documented above. Disparities across geographical regions and between urban and rural areas are often of primary importance in empirical studies of inequality in Brazil.²¹ To answer questions about the overall level of inequality in Brazil, our nationally representative sample is the appropriate level of analysis. Analysis by regions is, in effect, a study of within-region inequality, whereas we want to examine both within- and between-region variance in the distribution of earnings. A national sample also avoids the serious problem of internal migration, known to vary systematically with

²⁰ Estimates of returns to schooling may be biased for a variety of reasons, such as omitted family background or ability. Behrman and Wolfe (1984), for example, conclude from evidence on siblings in Nicaragua that estimates of returns to schooling are significantly overstated when family-related background characteristics are not controlled for. We see no reason to expect systematic relationship between these potential biases and age or cohort, however.

²¹ See, for example, Almeida Reis and Barros (1989).

age, education, and earnings. Age groups within one region may give a poor representation, for example, of the schooling history of men born in that region.

Nonetheless, it is interesting to see whether the patterns we describe above hold within regions. Using the 1985 PNAD we generated results equivalent to Tables 1 and 2 for two very different regions of Brazil, the Northeast and the Southeast, with further stratification for rural-urban location.²² We find changes in the distribution of schooling within the Northeast and Southeast similar to those for Brazil as a whole. We observe steady increases in mean schooling and steady declines in mean-adjusted schooling inequality over time for both rural and urban areas in both regions. We observe a peak in the variance of schooling similar to that for all of Brazil in the Southeast region overall and in Southeast urban areas. Northeast urban areas and the Northeast overall show patterns of rising, peaking, then falling variance, although the peaks are for somewhat younger cohorts than for Brazil as a whole. Rural areas in both regions have much lower variances in schooling, which tends to rise throughout the four decades. Estimates of age-specific earnings equations for rural and urban areas of the Southeast and Northeast indicate age profiles of inequality strikingly similar to those for Brazil as a whole. Within regions we find the same pattern of increasing returns to schooling with age as seen in Figure 7 for all Brazil. We also find that the pattern of increasing residual variance with age holds within these regions and their urban and rural areas. On the whole, the patterns in the age profiles of earnings inequality for all of Brazil appear quite robust across regions, in spite of the large differences in the overall levels of schooling and earnings in these regions.

Conclusions

Analysis of three-year age groups from the 1985 PNAD indicates that cohorts of Brazilian males born in the four decades between 1925 and 1963 experienced steady increases in the mean level of schooling, with the mean doubling from the oldest cohort to the youngest. This rising mean was associated with steady declines in schooling inequality. The coefficient of variation in years of schooling declined for every successive cohort, falling by almost 50 percent from the oldest cohort to the youngest. Lorenz curves for years of schooling demonstrate an unambiguous decline in mean-adjusted schooling inequality. The variance in years of schooling, a critical determinant of earnings inequality, increased for the first two decades of this period, reached a peak with the 1949-51 cohort, and has declined for all succeeding cohorts.

Estimates of separate earnings equations for three-year age groups in 1985 indicates that changes in the distribution of schooling in Brazil should in and of themselves have improved the distribution of labor earnings in Brazil beginning with cohorts born in the early 1950's. Earnings inequality falls dramatically from the 1946-48 cohort to the 1961-63 cohort, a pattern that is predicted by the declining variance in years of schooling over this period. Decomposition of the earnings equations reveals that two other factors play an important role in explaining this decline, however. Both returns to schooling and residual variance are higher for older cohorts, making

²² See Lam and Levison (1989) for detailed analysis of these regional comparisons.

inequality rise rapidly with age (i.e. fall with birth cohort). These two effects reinforce the effect of changes in the variance of schooling on earnings inequality.

Comparison of age and cohort profiles of inequality for 1976, 1982, and 1985 show that earnings inequality in Brazil increased over this period, in spite of the beneficial changes in the distribution of schooling. Our decomposition indicates that the contribution of schooling was in fact to improve the distribution from 1976 to 1985, with declines in both the variance of schooling and in the returns to schooling. These improvements were more than offset, however, by increases in other sources of inequality. Although the increase from 1976 to 1985 in the variance of the component of earnings that is uncorrelated with schooling is disturbing, we believe that our results regarding the schooling component of inequality provide reason for optimism about the future of earnings inequality in Brazil. While residual variance is likely to be sensitive to short-run economic conditions, the dramatic improvements in the distribution of schooling we document represent fundamental changes in the determinants of earnings inequality in Brazil. Our results suggest that changes in the distribution of schooling in Brazil in recent decades have had beneficial effects on the distribution of income, effects that should continue to be seen for decades. The decline in the variance of schooling that began for males born around 1950 implies that new cohorts entering the labor market should experience lower earnings inequality at every age, with past improvements in the schooling distribution having an increasingly equalizing effect on overall earnings inequality as post-1950 birth cohorts become an increasing proportion of the labor force.

Evidence cited earlier suggests that Brazil's recent experience of both increasing mean schooling levels and declining inequality in schooling is not unique among developing countries. This suggests that our findings may have implications beyond Brazil. To the extent that educational expansion in other developing countries reduces the variance in schooling variance, as appears to have occurred in Brazil, improvements in earnings inequality should result. If, in addition, there is a decline in returns to schooling, as also appears to have happened in Brazil, there will be further improvements in the distribution of earnings. Unfortunately, Brazil's recent experience also demonstrates that even substantial improvements in the schooling component of earnings inequality do not guarantee overall declines in inequality. Hopefully these are short-run cyclical effects that will in the long-run be dominated by the structural improvements in the distribution of schooling.

APPENDIX

Table A. Distribution of Earnings for Three-Year Age Groups
Brazilian Males with Positive Earnings, 1976 and 1982 PNAD

Age	1976 PNAD					1982 PNAD				
	<i>N</i>	<i>V(ln Y)</i>	$\hat{\beta}$	R^2	<i>V(u)</i>	<i>N</i>	<i>V(ln Y)</i>	$\hat{\beta}$	R^2	<i>V(u)</i>
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)
22-24	8740	0.631	0.117	0.304	0.439	11487	0.558	0.107	0.305	0.388
25-27	8184	0.791	0.138	0.411	0.466	10862	0.721	0.127	0.408	0.427
28-30	7829	0.931	0.156	0.467	0.496	10283	0.817	0.141	0.464	0.438
31-33	6256	1.007	0.167	0.499	0.505	9386	0.936	0.153	0.508	0.460
34-36	6356	0.953	0.167	0.425	0.548	8246	1.017	0.156	0.515	0.493
37-39	5730	0.970	0.165	0.433	0.550	7262	1.014	0.160	0.504	0.503
40-42	5563	1.007	0.170	0.434	0.570	7066	1.020	0.167	0.490	0.521
43-45	4735	1.032	0.174	0.437	0.581	5991	1.023	0.171	0.467	0.545
46-48	4410	1.052	0.176	0.419	0.611	5202	1.056	0.167	0.434	0.598
49-51	3811	1.051	0.181	0.415	0.615	4556	1.066	0.172	0.437	0.600
52-54	3223	1.095	0.181	0.406	0.651	4179	1.023	0.171	0.414	0.600
55-57	2424	1.064	0.178	0.361	0.680	3367	1.016	0.163	0.348	0.662
58-60	2075	1.130	0.187	0.397	0.681	2579	1.014	0.168	0.384	0.624
22-60	69336	0.951	0.152	0.385	0.585	90466	0.921	0.142	0.408	0.545

See Table 2 notes.

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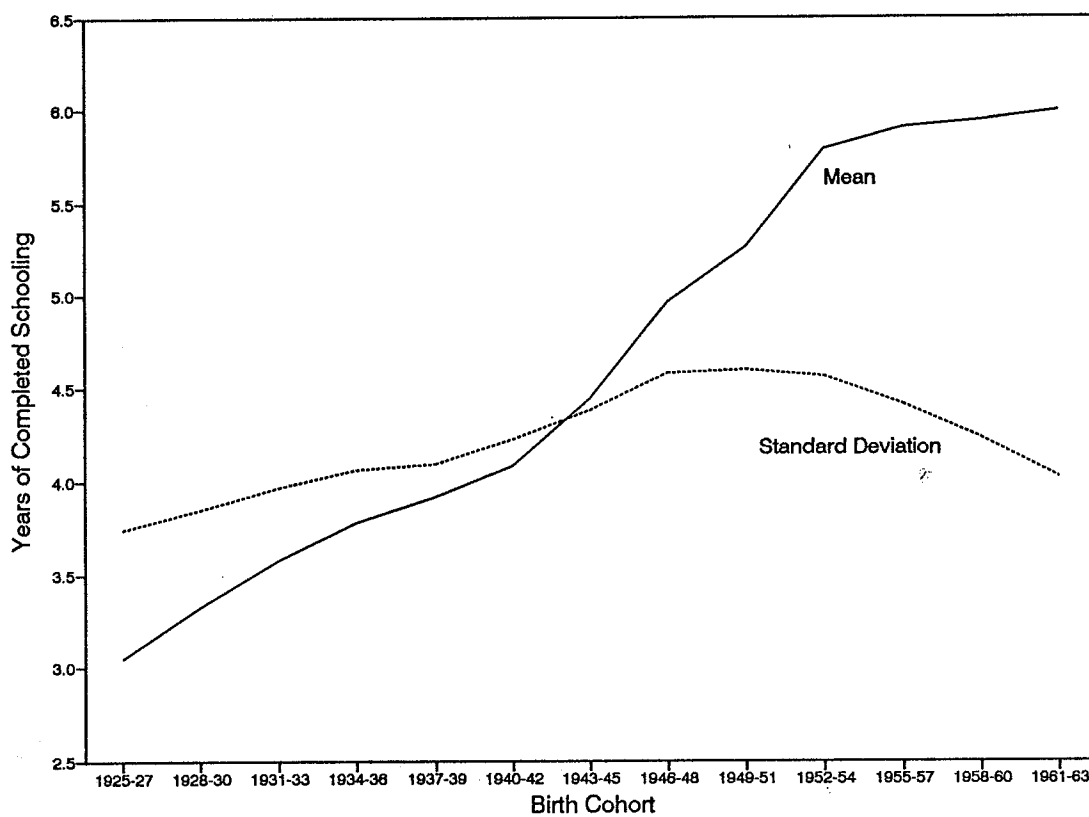


Figure 1.
Years of Completed Schooling, Mean and Standard Deviation
Three-Year Birth Cohorts, Brazilian Males, 1985 PNAD

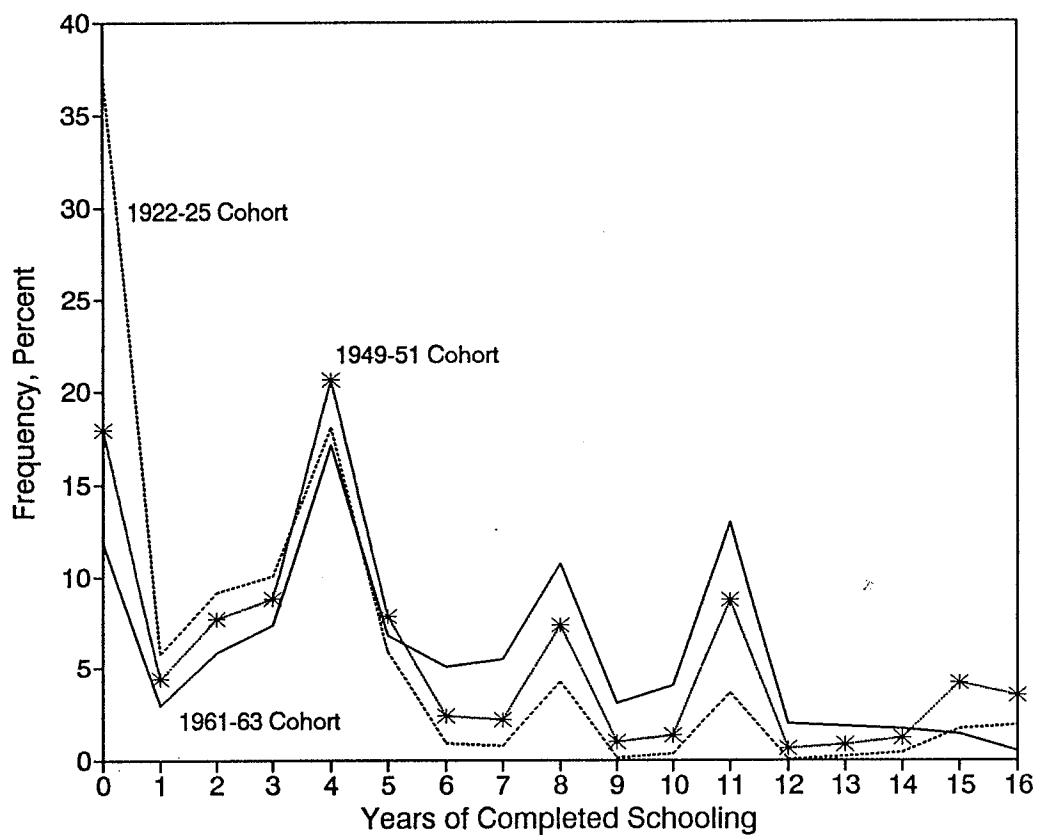


Figure 2.
Frequency Distribution, Years of Completed Schooling
1925-27, 1949-51, and 1961-63 Birth Cohorts, Brazilian Males, PNAD 1985

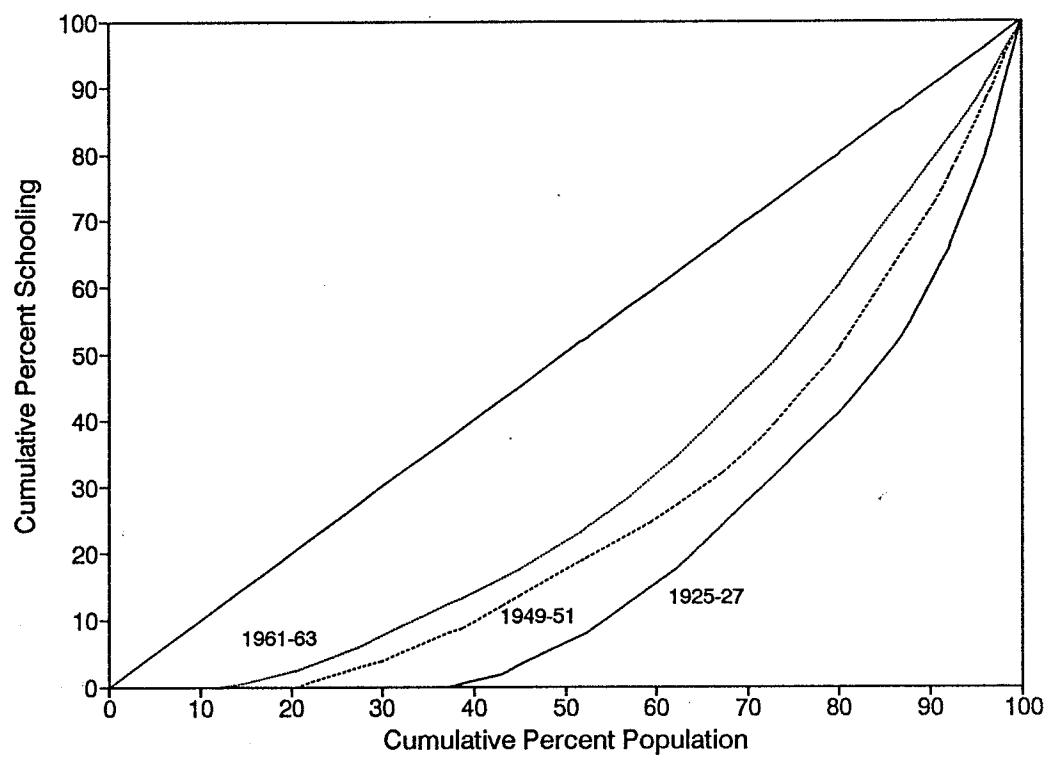


Figure 3.
Lorenz Curves, Years of Completed Schooling
1925-27, 1949-51, and 1961-63 Birth Cohorts, Brazilian Males, PNAD 1985

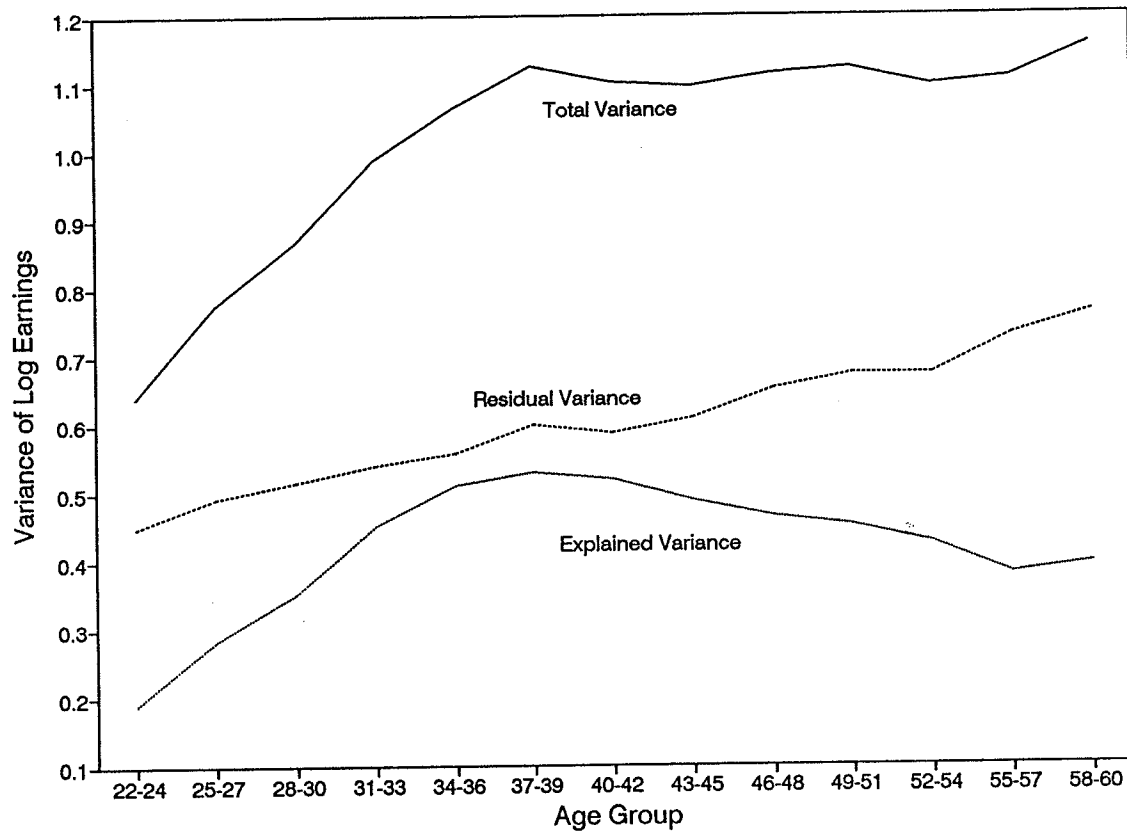


Figure 4.
 Earnings Inequality, Three-Year Age Groups
 Total Variance of Log Earnings, Explained Variance, and Residual Variance
 Males with Positive Earnings, All Brazil, PNAD 1985

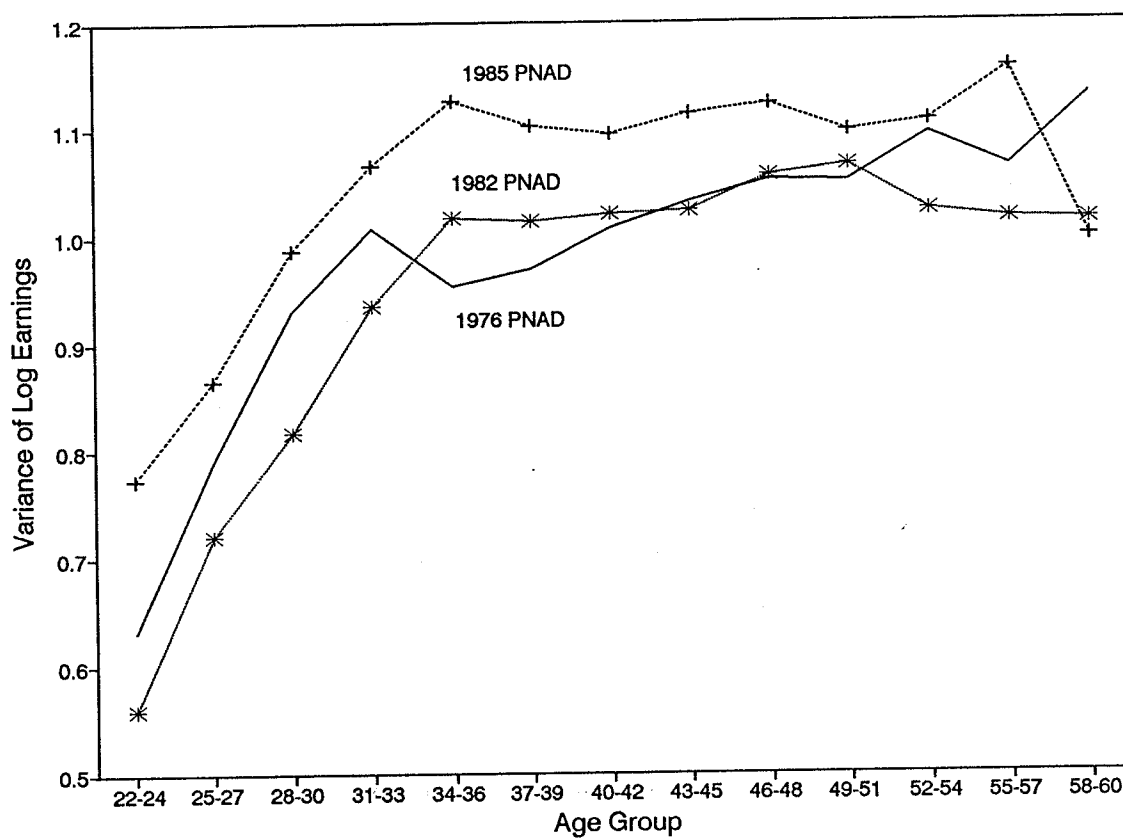


Figure 5.
 Variance in Log Earnings for Three-Year Age Groups
 Brazilian Males with Positive Earnings, PNAD 1976 — 1982 — 1985

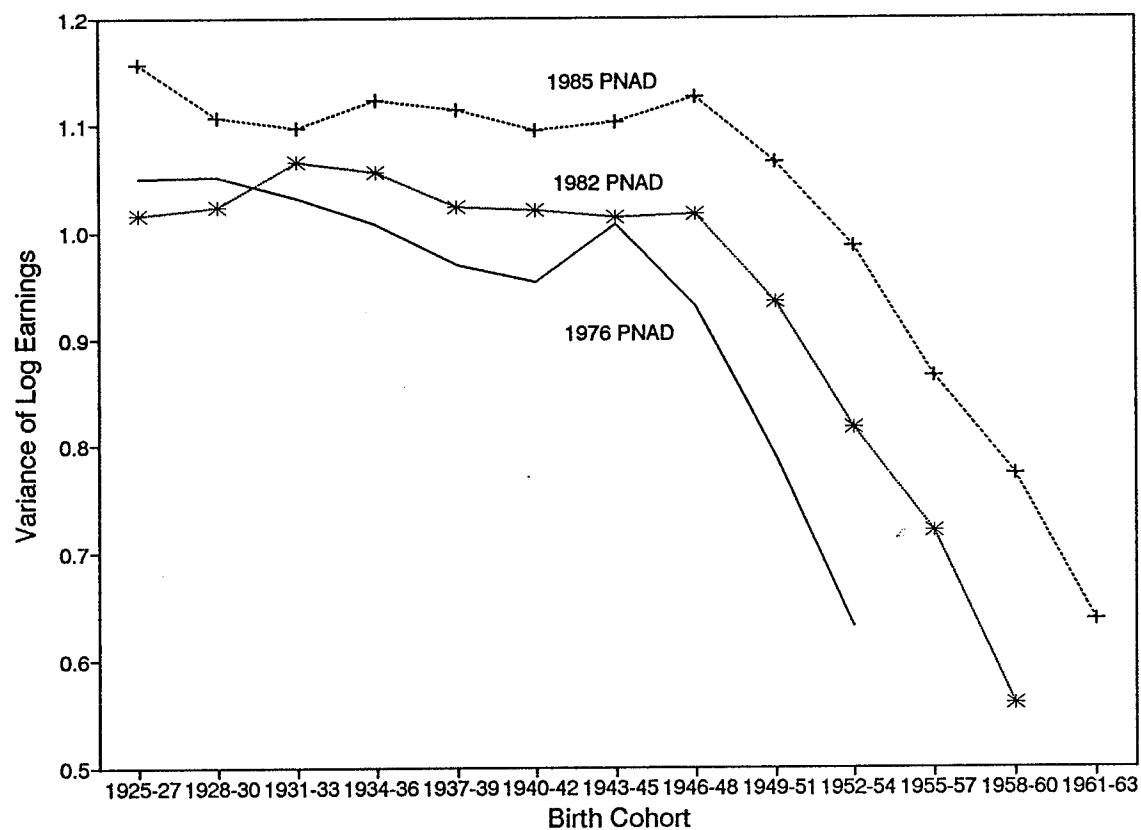


Figure 6.
 Variance in Log Earnings for Three-Year Birth Cohorts
 Brazilian Males with Positive Earnings, PNAD 1976 — 1982 — 1985

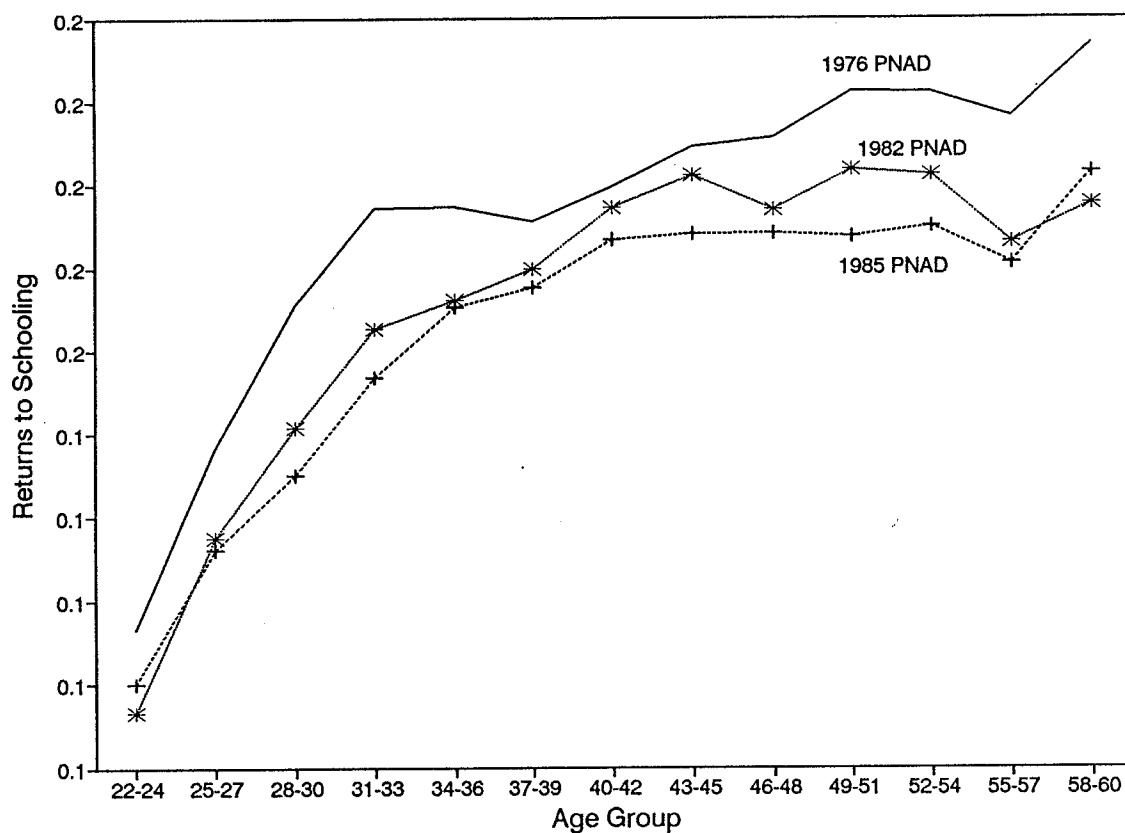


Figure 7.
 Estimated Returns to Schooling for Three-Year Age Groups
 Brazilian Males with Positive Earnings, PNAD 1976 — 1982 — 1985

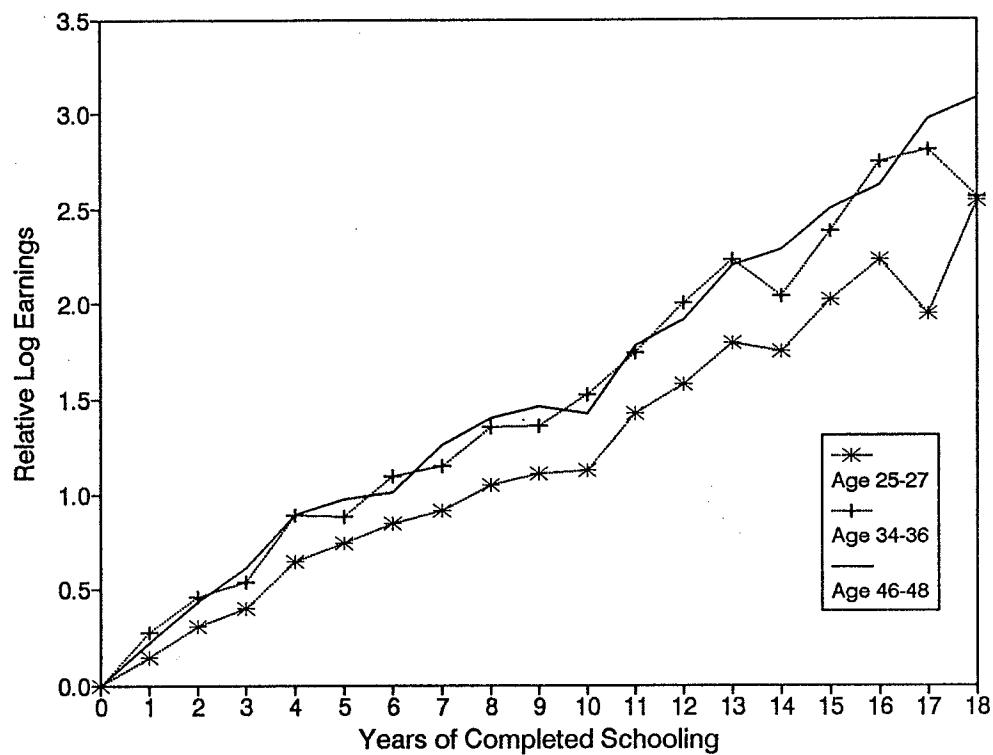


Figure 8.
 OLS Regressions Using Single Year of Completed Schooling
 Log Earnings Relative to Males with Zero Years of Completed Schooling
 Three-Year Age Groups, Brazilian Males with Positive Earnings, 1985 PNAD