

Coordination Risk and the Price of Debt*

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Abstract

Creditors of a distressed borrower face a coordination problem. Even if the fundamentals are sound, fear of premature foreclosure by others may lead to pre-emptive action, undermining the project. Recognition of this problem lies behind corporate bankruptcy provisions across the world, and it has been identified as a culprit in international financial crises, but has received scant attention from the literature on debt pricing. The apparent multiplicity of equilibria is a barrier to development of this issue in asset pricing, but this multiplicity is only apparent. Without common knowledge of fundamentals, the incidence of failure is uniquely determined provided that private information is precise enough. This affords a way to price the coordination failure. There are two further conclusions. First, coordination is more difficult to sustain when fundamentals deteriorate. Thus, when fundamentals deteriorate, the onset of crisis can be very swift. Second, “transparency” - in the sense of greater provision of information to the market - does not generally mitigate the coordination problem. Transparency is not a panacea.

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1. Introduction

Our premise in this paper is that creditors face a coordination problem when facing a borrower in distress, and that this will be reflected in the price of debt. The problem faced by creditors is akin to that faced by depositors of a bank which is vulnerable to a run. Even if the project is viable, so that the value at maturity is enough to pay all the creditors in full, a creditor may be tempted to foreclose on the loan or seize any assets it can, fearing similar actions by other creditors. Such fears would be self-fulfilling, since the disorderly liquidation of assets and the consequent disruption to the project is more likely to lead to failure of the project.

It is hard to overstate the importance of coordination failures. The recognition of this problem - known as the “common pool problem” among lawyers - lies at the heart of corporate bankruptcy provisions across the world, taking on its most elaborate form in the chapter 11 provisions of the U.S. bankruptcy code (Baird and Jackson (1990), Jackson (1986)). Also, coordination failure among creditors has been fingered by many commentators as the main culprit in the recent series of international financial crises. Both Fischer (1999) and Radelet and Sachs (1998) - whatever their other differences - attribute the Asian financial crisis of 1997 to coordination failure among creditors and other market participants.

Given the importance of this problem, it is incongruous that it has received scant attention from the literature on asset pricing. The main difficulty in incorporating the effects of the coordination problem in any pricing theory for debt is that coordination problems lead to multiple equilibria. Without quantifiable information on the incidence of coordination failure, it is impossible to incorporate this into the ex ante price of the debt in a rigorous way. Thus, the first step in measuring the pricing implications of coordination failure is to establish a theory which extracts a unique outcome as a function of underlying fundamentals. This is a precondition for the sort of analysis attempted here.

The events of 1997/8 have focused renewed attention on the problem of pricing debt, and have served as a reminder of some of the shortcomings in our current understanding of the topic. The late summer and autumn of 1998 were exceptionally turbulent times, and none more so than in the bond market. For corporate bonds, the yield spread over government bonds of comparable maturity widened sharply, as did the spread between high and low grade corporate bonds¹. Such spreads were

¹For U.S. corporate bonds below investment grade, the yield spreads over U.S. Treasury bonds of comparable maturity widened from about 3.75% in early August to around 6% by

almost without precedent - at least outside recessionary periods. This widening of spreads was also accompanied by the virtual drying up of new issues of corporate bonds, especially those below investment grade. Some of the more acute episodes of market disruption took on a 'systemic' character, in which there were spillovers from one market to another. To the extent that systemic risk reflects underlying coordination problems among market participants, understanding the nature of coordination failure is an important element in our understanding of these unprecedented events.

In many instances, coordination problems may be mitigated by suitable collateralization, or by arranging financing through a single lender or a small well-defined consortium of lenders. Many observers have noted how, even during the most turbulent periods in 1998, access to bank credit by firms was much less affected than their access to the bond market². However, for borrowers with large projects (or for sovereign borrowers) who must draw on many disparate lenders, such coordination problems may be important. Empirical studies of financial re-contracting of firms under distress suggest that instances of disorderly liquidation and deviations from priority of debtors may play a significant role (Franks and Torous (1994)).

Even before the events of 1997/8, it would be fair to say that the theories underlying the pricing of debt had not enjoyed the same broad consensus of support nor the empirical success of other applications of asset pricing theory. A classic reference in the theory of the valuation of debt is Merton (1974), which models company asset value as a geometric Brownian motion, and assumes that bankruptcy occurs when asset value reaches some given level. Then, the price of debt can be obtained from Black-Scholes pricing techniques applied to the terminal conditions implied by the payoffs of the debt contract. More refined treatments of this approach include Leland (1994) - recognizing debt level as a decision by the firm - and Longstaff and Schwartz (1995) - which allows interest rate risk.

However, the empirical success of this approach has been mixed. One early study is Jones, Mason and Rosenfeld (1984), which uses data from 1975 to 1981 and finds that the actual observed prices of corporate bonds are below those predicted by the theory, and that the prediction error is larger for lower rated

mid-October - the highest since the collapse of the U.S. junk bond market in the early 1990s. For highest rated (Aaa) investment grade bonds, the spreads widened from around 0.9% in early August to around 1.5% in mid-October. For bonds rated Baa, the spreads rose from around 1.5% to 2.3%. See IMF (1998a)

²See, for instance, the series of articles in the *Financial Times* and the *Wall Street Journal* in the week of October 16th 1998.

bonds. For investment grade bonds, the error is around 0.5%, while for non-investment grade bonds, the error is much larger, at around 10%. Subsequent work has suggested that over-pricing is resilient to refinements of the theory, and this has given rise to a number of more far-reaching departures from the classical model of Merton. Anderson and Sundaresan (1996) suggest that shifts in bargaining power between the creditors and managers may explain the price anomaly. An alternative approach is to assume that default is an exogenous event which follows some hazard rate process. Then, the default risk is reflected in a higher discount rate. Duffie and Singleton (1999) develop this approach.

In our paper, we formulate a theory which attempts to explain the incidence of coordination failure as a function of the underlying fundamentals and other relevant parameters. Once this incidence can be calculated, it is then a matter of evaluating the ex ante value of coordination failure and incorporating this risk into the price of debt. This framework allows us to address two issues of current debate - the proper use of value at risk (VaR) analysis, and the role (if any) of greater ‘transparency’ in preventing market turbulence.

Value at risk analysis attempts to quantify the potential impact on the value of a portfolio of shifts in the underlying state. However, the current state of the art does not make any explicit provision for coordination failure. By quantifying the impact of coordination failure, it is possible to formulate a framework for credit risk analysis which addresses some of the ‘systemic’ issues. To anticipate our key finding, we show that when the fundamental viability of a loan deteriorates, the coordination problem becomes more acute, so that the ex ante asset value of the loan falls more than proportionately to the deterioration of the fundamentals. We dub this additional effect the ‘coordination effect’. It reinforces the conventional effect in which a shift in the payoff distribution increases the weight of the left tail of the distribution. The size of the coordination effect depends on the parameters of the problem.

Transparency has become a touchstone of the policy response following the events of 1997/8. Although the notion of transparency is sometimes difficult to pin down, it has generally been taken to mean the provision of more accurate and timely information to market participants. The unstated premise in the call for more transparency is that the improved provision of information will mitigate coordination failure. One of the possibilities opened up by our framework is that we can subject this premise to more rigorous scrutiny. To anticipate our main conclusion, we find little to suggest that the provision of more accurate information improves matters. The effect of improved information on the efficiency

of the outcome is ambiguous at best. This raises some important issues in the policy debate. When calling for improved transparency, it is important to be clear as to *how* the improved information will improve the outcome. The mere provision of information is unlikely to mitigate coordination failure. Rather, the institutional backdrop will be important in the way that transparency affects the market outcome. It is perhaps no accident that instances of successful coordination by creditors have had a forceful facilitator organizing the bailout - such as the New York Fed in the rescue of Long Term Capital Management in 1998, or the U.S. Treasury in the aftermath of the Korean financial crisis of 1997/8. Instances of voluntary coordination when there is no such facilitator are much more difficult to find.

2. The Model

A group of creditors are financing a project. Each creditor is small in that an individual creditor's stake is negligible as a proportion of the whole. We index the set of creditors by the unit interval $[0, 1]$. At the end of its term, the project yields a liquidation value v , which is uncertain at the time of investment. The financing is undertaken via a standard debt contract. The face value of the repayment is L , and each creditor receives this full amount if the realized value of v is large enough to cover repayment of debt.

At an interim stage, before the final realization of v , the creditors have an opportunity to review their investment. The loan is secured on collateral, whose liquidation value is $K^* < L$ if it is liquidated at the interim stage, but has the lower value K_* if it is liquidated following the project's failure. Thus,

$$K_* < K^* < L$$

At the interim stage, each creditor has a choice of either rolling over the loan until the project's maturity, or seizing the collateral and selling it for K^* . The value of the project at maturity depends on two factors - the underlying state θ , and the degree of disruption caused to the project by the early liquidation by creditors. Denoting by ℓ the proportion of creditors who refuse to roll over the loan at the interim stage, the realized value of the project is given by

$$v(\theta, \ell) = \begin{cases} V & \text{if } z\ell \leq \theta \\ K_* & \text{if } z\ell > \theta \end{cases} \quad (2.1)$$

where V is a constant greater than L , and $z > 0$ is a parameter which measures the severity of disruption caused by early liquidation.

By normalizing the payoffs so that $L = 1$ and $K_* = 0$, the payoffs to a creditor are given by the following matrix, where $\lambda \equiv (K^* - K_*) / (L - K_*)$.

	Project succeeds	Project fails
Roll over loan	1	0
Foreclose on loan	λ	λ

[Figure 1 here]

The bold line in figure 1 depicts the payoff to a creditor arising from the loan when proportion ℓ refuse to roll over the loan.

To avoid notational clutter, we assume that if rolling over the loan yields the same expected payoff as foreclosing on the loan, then a creditor prefers to foreclose. This assumption plays no substantial role.

If the creditors know the value of θ perfectly before deciding on whether to roll over the loan, their optimal strategy can be analysed thus. If $\theta > z$, then it is optimal to continue with the project, irrespective of the actions of the other creditors. This is so, since even if every other creditor recalls the loan, the project yields enough to pay back the full face value of the loan (equal to 1). This is more than λ . Conversely, if $\theta < 0$, then it is optimal to recall the loan irrespective of the actions of the others. Even if all other creditors roll over their loans, the project yields zero, which less than λ .

When θ lies in the interval $(0, z)$, there is a coordination problem among the creditors. We may think of this interval as the set of states in which a “credit event” has occurred, and in which the creditors are in a position to seize assets if they so chose. If all other creditors roll over their loan, then the payoff to rolling over the loan is 1, so that rolling over the loan to maturity yields more than the premature liquidation value λ . However, if everyone else recalls the loan, the payoff is $0 < \lambda$, so that early liquidation is optimal. This type of coordination problem among creditors is analogous to the bank run problem (Diamond and Dybvig (1983)), and leads to multiple equilibria in the simple perfect information game in which creditors choose their actions when θ is common knowledge³.

³We do not have much to add to the debate on whether a secondary market will mitigate inefficiencies, except to note that any attempt to internalize the externalities are confronted by coordination/free-rider problems at a higher level. See Gertner and Scharfstein (1991).

Based on the structure outlined above, we proceed to develop a model of credit under imperfect information. When the creditors make their initial investment, they know that θ is normally distributed with mean y , and precision α (that is, with variance $1/\alpha$). At the interim stage, when each creditor decides on whether to roll over the loan, each creditor receives information concerning θ , but this information is imperfect. Creditor i observes the realization of the noisy signal

$$x_i = \theta + \varepsilon_i \tag{2.2}$$

where ε_i is normally distributed with mean 0 and precision β . For $i \neq j$, ε_i and ε_j are independent.

A *strategy* for creditor i is a decision rule which maps each realization of x_i to an action (i.e. to roll over the loan, or to foreclose on the loan prematurely). An *equilibrium* is a profile of strategies - one for each creditor - such that a creditor's strategy maximizes his expected payment conditional on the information available, when all other creditors are following the strategies in the profile.

We have noted that when θ is observed perfectly (so that $x_i = \theta$), there is more than one equilibrium. Indeed, there is an (uncountable) infinity of equilibria in this case. When θ is observed imperfectly, there is a unique equilibrium provided that the noise ε_i is sufficiently small, as we now demonstrate.

3. Unique Equilibrium

When creditor i observes the realization of the signal x_i , his posterior distribution of θ is normal with mean

$$\xi_i \equiv \frac{\alpha y + \beta x_i}{\alpha + \beta} \tag{3.1}$$

and precision $\alpha + \beta$. We can then state the following result.

Theorem 1. If $\alpha/\sqrt{\beta} \leq \sqrt{2\pi}/z$, there is a unique equilibrium. Conversely, if $\alpha/\sqrt{\beta} > \sqrt{2\pi}/z$, there is a value of λ such that there is more than one equilibrium.

In interpreting this result, it is useful to consider the ex ante distribution of θ as public information concerning θ , distinguishing it from the private signal x_i . When the precision of the private signal (given by β) becomes large while fixing the precision of the public signal, we are guaranteed a unique equilibrium. Conversely, when the private signal is *not* sufficiently informative, then multiplicity

of equilibrium re-emerges for some parameter values of the problem. The critical level of the informativeness of the private signal can be given a characterization in terms of whether $\alpha/\sqrt{\beta}$ is smaller or larger than $\sqrt{2\pi}/z$.

3.1. Preliminaries

Let us begin by considering the following hypothetical situation. Suppose there is some given level ξ of the posterior belief of the state θ such that every creditor rolls over the loan if and only if his posterior belief is higher than ξ . Then consider the expected payoff of rolling over the loan when one's posterior belief is exactly equal to ξ . In other words, consider the expected payoff from rolling over the loan at the switching point. Denote this payoff by $U(\xi)$. Our result on uniqueness is a consequence of the following pair of results.

Lemma 1. If ξ solves $U(\xi) = \lambda$, then there is an equilibrium in which everyone employs the switching strategy around ξ . If there is a unique ξ which solves $U(\xi) = \lambda$, then there is no other equilibrium.

Lemma 2. $U'(\xi) \geq 0$ for all ξ if and only if $\alpha/\sqrt{\beta} \leq \sqrt{2\pi}/z$.

The first lemma draws on recent analysis of games without common knowledge of payoffs⁴. In fact, we shall prove a much stronger result - namely, that if there is a unique solution to $U(\xi) = \lambda$, then the switching strategy around ξ is the only strategy which survives the iterated deletion of dominated strategies. The general structure of our model conforms to the class of supermodular games examined by Milgrom and Roberts (1990), and it is illuminating to see the uniqueness result in this light. The details are presented in the appendix.

As for the second lemma, we give the proof here. If ℓ is determined by everyone following the switching strategy around ξ , what is the critical value of θ for which the project succeeds? In other words, we want the θ which solves

$$\theta = z\ell \tag{3.2}$$

⁴The work of Rubinstein (1989) and Monderer and Samet (1989) was followed by Carlsson and Van Damme (1993a, b), who introduced the notion of "global games". Morris, Rob and Shin (1995), and Kajii and Morris (1997) develop these results. Morris and Shin (1997) is a survey of some of the early results. Morris and Shin (1998a, b) apply these results in the analysis of currency attacks.

From (3.1), the switching strategy around ξ entails rolling over the loan if and only if the private signal x is greater than

$$x(\xi, y) \equiv \frac{\alpha + \beta}{\beta} \xi - \frac{\alpha}{\beta} y. \quad (3.3)$$

At state θ , the distribution of x is normal with mean θ and precision β . Hence, the proportion of creditors who have a signal lower than (3.3) is given by the area under this density up to x . Hence,

$$\ell = \Phi \left(\sqrt{\beta} (x(\xi, y) - \theta) \right) \quad (3.4)$$

where $\Phi(\cdot)$ is the cumulative distribution function for the standard normal. Substituting into (3.2), we have an expression for the critical value of θ at which the project succeeds. That is,

$$\theta = z \Phi \left(\sqrt{\beta} (x(\xi, y) - \theta) \right) \quad (3.5)$$

This value of θ is unique⁵, and is a function of ξ and y , and so we write

$$\psi(\xi, y) \quad (3.6)$$

as the unique value of θ which solves (3.5). $\psi(\xi, y)$ satisfies

$$\psi(\xi, y) = z \Phi \left(\sqrt{\beta} (x(\xi, y) - \psi(\xi, y)) \right) \quad (3.7)$$

Now, the payoff $U(\xi)$ is given by

$$\begin{aligned} U(\xi) &= \int_{\psi}^{\infty} \phi \left(\sqrt{\alpha + \beta} (\theta - \xi) \right) d\theta \\ &= 1 - \Phi \left(\sqrt{\alpha + \beta} (\psi - \xi) \right) \end{aligned} \quad (3.8)$$

so that

$$U'(\xi) = -\sqrt{\alpha + \beta} \cdot \phi \left(\sqrt{\alpha + \beta} (\psi - \xi) \right) \cdot \left(\frac{\partial \psi}{\partial \xi} - 1 \right) \quad (3.9)$$

⁵The uniqueness follows from the fact that the right hand side is decreasing in θ , continuous, and takes all values in the open interval $(0, 1)$. Hence there is a unique point at which it cuts the 45^o line.

where $\phi(\cdot)$ is the density of the standard normal. Hence $U'(\xi) \geq 0$ if and only if $\frac{\partial \psi}{\partial \xi} \leq 1$. By implicit differentiation of (3.7) with respect to ξ ,

$$\frac{\partial \psi}{\partial \xi} = z\sqrt{\beta} \left(\frac{\alpha + \beta}{\beta} - \frac{\partial \psi}{\partial \xi} \right) \phi \left(\sqrt{\beta}(x - \psi) \right)$$

Solving for $\frac{\partial \psi}{\partial \xi}$, we have

$$\frac{\partial \psi}{\partial \xi} = \frac{\phi\sqrt{\beta}}{\frac{1}{z} + \phi\sqrt{\beta}} \cdot \frac{\alpha + \beta}{\beta}$$

Thus, $\frac{\partial \psi}{\partial \xi} \leq 1$ if and only if

$$\frac{\phi\sqrt{\beta}}{\frac{1}{z} + \phi\sqrt{\beta}} \leq \frac{\beta}{\alpha + \beta} \quad (3.10)$$

Since the left hand side is maximized at $\phi = 1/\sqrt{2\pi}$, a sufficient condition for $\frac{\partial \psi}{\partial \xi} \leq 1$ is

$$\frac{\sqrt{\beta}}{\frac{\sqrt{2\pi}}{z} + \sqrt{\beta}} \leq \frac{\beta}{\alpha + \beta}$$

which boils down to

$$\alpha/\sqrt{\beta} \leq \sqrt{2\pi}/z.$$

Conversely, suppose $\alpha/\sqrt{\beta} > \sqrt{2\pi}/z$. Then, from (3.10), $\frac{\partial \psi}{\partial \xi} > 1$ when $x = \psi$. This proves the lemma.

4. Default

We proceed to characterize the unique equilibrium. The failure point ψ depends on the strategies used by the creditors, but it is equally clear that the optimal strategy for a creditor depends on his beliefs about the failure point. Thus, characterizing the equilibrium involves solving - simultaneously - for the failure point ψ and the optimal strategy.

In the unique equilibrium, theorem 1 tells us that all creditors employ the switching strategy around ξ , where ξ is the unique solution to

$$U(\xi) = \lambda \quad (4.1)$$

The critical state at which the project succeeds is the θ for which $\theta = z\ell$, where ℓ is generated by the equilibrium switching strategy. From (3.7), the critical state ψ satisfies the equation:

$$\begin{aligned}\psi &= z\Phi\left(\sqrt{\beta}(x - \psi)\right) \\ &= z\Phi\left(\sqrt{\beta}\left(\frac{\alpha+\beta}{\beta}\xi - \frac{\alpha}{\beta}y - \psi\right)\right) \\ &= z\Phi\left(\frac{\alpha}{\sqrt{\beta}}(\xi - y) + \sqrt{\beta}(\xi - \psi)\right)\end{aligned}\tag{4.2}$$

Meanwhile, from (4.1) we have

$$1 - \Phi\left(\sqrt{\alpha + \beta}(\psi - \xi)\right) = \lambda\tag{4.3}$$

so that (4.2) and (4.3) give us two equations in our two unknowns, ψ and ξ . From (4.3),

$$\psi - \xi = \frac{\Phi^{-1}(1 - \lambda)}{\sqrt{\alpha + \beta}}\tag{4.4}$$

Denoting $k \equiv -\Phi^{-1}(1 - \lambda)$, and solving for ψ , we have

$$\psi = z\Phi\left(\frac{\alpha}{\sqrt{\beta}}\left(\psi - y + k\frac{\sqrt{\alpha+\beta}}{\alpha}\right)\right).\tag{4.5}$$

The failure point ψ is obtained as the intersection between the 45° line and a scaled-up cumulative normal distribution whose mean is $y - k\frac{\sqrt{\alpha+\beta}}{\alpha}$, and whose precision is α^2/β . From theorem 1, we know that there is precisely one point of intersection, since equilibrium is unique⁶. When z is large, the destruction of value can be very substantial. The interval $[0, \psi]$ represents the size of the inefficiency.

[Figure 2 here]

The failure point ψ depends on the parameters of the problem. We note that

- ψ is increasing in λ
- ψ is increasing in z
- ψ is decreasing in y , the ex ante mean of θ .

⁶This is reflected in (4.5) by the fact that the slope of the expression on the right is less than one when $\alpha/\sqrt{\beta} \leq \sqrt{2\pi}/z$.

Thus, failure occurs at higher values of the fundamentals if the collateral has high liquidation value, when the success of the project is more fragile to the early liquidation of creditors, and when the debt is of low quality. The fact that failure is more likely when y is low is an important result, and we turn to this now.

4.1. Value at Risk

Let us begin by verifying that the failure point ψ does indeed move in the opposite direction to y . Differentiate (4.5) to obtain

$$\frac{\partial \psi}{\partial y} = z \frac{\alpha}{\sqrt{\beta}} \left(\frac{\partial \psi}{\partial y} - 1 \right) \phi$$

so that

$$\frac{\partial \psi}{\partial y} = - \frac{\frac{\alpha}{\sqrt{\beta}} z \phi}{1 - \frac{\alpha}{\sqrt{\beta}} z \phi} \quad (4.6)$$

But the denominator is positive, since uniqueness implies (by Theorem 1) $\alpha/\sqrt{\beta} \leq \sqrt{2\pi}/z$, and ϕ is bounded above by $1/\sqrt{2\pi}$. Hence,

$$\frac{\partial \psi}{\partial y} < 0.$$

Consider a numerical examples with $\lambda = 1/2$ and $z = 1$ where we plot the failure point ψ as a function of y . The largest value of $\alpha/\sqrt{\beta}$ which ensures uniqueness is $\sqrt{2\pi} \approx 2.5$. The function $\psi(y)$ for this value is given by the steepest line in figure 4. The figure also plots ψ for $\alpha/\sqrt{\beta}$ taking the values 1 and 0.4. As $\alpha/\sqrt{\beta} \rightarrow 0$, $\psi(y)$ tends to the constant function passing through $1/2$.

[Figure 4 here]

As a comparison, it should be borne in mind that the benchmark model which ignores coordination risk is equivalent to assuming that the failure point ψ is the constant function through zero.

The fact that the failure point moves up as the fundamentals deteriorate has far-reaching consequences for risk management. For example, consider the value of an *unsecured* loan to the project with face value 1. The owner of such an asset only receives a positive payoff when the true state is higher than ψ . The ex ante price of such a loan given ex ante mean y is

$$W(y) = \int_{\psi}^{\infty} \phi(\sqrt{\alpha}(\theta - y)) d\theta = 1 - \Phi(\sqrt{\alpha}(\psi - y)) \quad (4.7)$$

For the owner of this asset who wishes to calculate the possible changes in price, one important consideration is how ψ changes with shifts in the ex ante mean y of the project. Value at risk analysis can be seen as an attempt to quantify the possible changes in price as y changes. The change in the asset value of the loan to a shift in the mean of the distribution is

$$\frac{\partial W}{\partial y} = \sqrt{\alpha} \cdot \phi - \frac{\partial \psi}{\partial y} \sqrt{\alpha} \cdot \phi \quad (4.8)$$

The first term could be dubbed the *conventional effect* in that it reflects the change in the weight of the left tail of the distribution due to a shift in the centre of the distribution. The second term is the novel feature. It arises from the fact that the threshold for the tail also shifts. We could call this the *coordination effect*. Since $\partial\psi/\partial y < 0$, the coordination effect reinforces the conventional effect. Figure 3 illustrates the two effects.

[Figure 3 here]

As a function of y , the critical value ψ is decreasing in y . As the fundamentals deteriorate from y to \hat{y} , the critical value of the state shifts to the *right* from ψ to $\hat{\psi}$. Thus, the asset value of the loan falls for two reasons. For a fixed threshold, the distribution puts more weight on the lower tail. This is the conventional effect, and is indicated as the area A. The second effect arises from the fact that the critical threshold moves up, also. This is the coordination effect, and is indicated by the area B.

For the creditor, a deterioration in the fundamentals in terms of a fall in y implies that the asset value of the loan is falling at a rate *more than proportional* to the fall in y . Thus, it is precisely when risk management is most important - when y is falling - that it is important not to neglect the coordination effect. By neglecting the coordination effect, the creditor is underestimating the true value at risk.

4.2. Numerical Example

Defining the yield on the unsecured loan as

$$\text{Yield} = \frac{\text{Par} - \text{Price}}{\text{Price}},$$

we can compare the yields generated by the true model (with failure occurring at ψ) with the yields given by the naive model which assumes away coordination

risk. The following table is generated from the case where

$$\alpha = 1, \quad \beta = 5, \quad z = 1, \quad \lambda = 0.5.$$

The first column gives the ex ante mean of the payoff distribution and the second column gives the yield on the loan for the naive model (no coordination risk). The third column gives the yield arising from the true model, and the value of the break point $\psi(y)$ appears in the last column. Since $\alpha = 1$, the values of y are in units of standard deviations. So, the first row of the table pertains to the case where the ex ante mean y is three standard deviations from zero - the failure point in the naive model. The last element of this row tells us that the true failure point is $\psi(3) = 0.097$, and the true yield is 0.19%, rather than the yield given by the naive model of 0.14%. This difference in yield is not large, since the loan is a very safe one - the mean being three standard deviations away from zero.

Ex ante mean y	Yield from naive model	Yield from true model	Failure point ψ
$y = 3$	0.0014	0.0019	0.097
$y = 2$	0.0233	0.0383	0.212
$y = 1.5$	0.0716	0.1288	0.295
$y = 1.25$	0.1181	0.2226	0.342
$y = 1$	0.1886	0.3735	0.393
$y = 0.75$	0.293	0.6143	0.446
$y = 0.5$	0.4462	1.0	0.5
$y = 0.25$	0.6703	1.6279	0.554
$y = 0$	1.0	2.6774	0.607

However, as y falls, we can see that the yield difference becomes large. At one standard deviation away from zero (i.e. for $y = 1$), the naive model predicts a yield of 19%, but the true yield is actually almost double that number, at 37%. This corresponds to the break point of $\psi = 0.393$. For even lower values of y , the yield difference is even higher. When $y = 0$, the naive model predicts a yield of 100%, but the true yield is 268%.

5. Transparency

The detrimental effect of imperfect information on the asset value of the loan can be sizeable. It is therefore pertinent to ask whether, and by how much, the damage

can be limited by improvements in the information of the market participants. The term “transparency” has taken on great significance in the policy debate after the market turmoil of 1997/8, and has figured prominently in numerous official publications (such as IMF (1998b)). Although the notion of transparency is sometimes difficult to pin down exactly, it is generally taken to mean the provision of more accurate and timely information to market participants. The unstated premise in the call for more transparency is that the improved provision of information will enable market participants to act in such a way that the destruction of value through imperfect coordination can be minimized.

Having developed the framework so far, we are now in a position to subject this premise to more rigorous scrutiny. To anticipate our main conclusion, we find little to suggest that the provision of more accurate information improves matters. The effect of improved information on the efficiency of the outcome is ambiguous at best.

We consider two cases of improvement of information. In the first, we envisage the creditors’ private information as being very accurate as to the underlying state θ relative to the public information. We formalize this in terms of the precision β of the private signals become infinite while α remains fixed. In the second, we envisage the case where both the private and public information improve in tandem. Since the creditors will always have access to some private information, we model this situation by letting both α and β become large, but where β increases at the rate of α^2 .

5.1. Case of Precise Private Information

When the noise in the creditors’ signals become small, each creditor has good information about the underlying state θ . What happens in the limit when the noise becomes negligible? This corresponds to the case where the precision β becomes large relative to α . From (4.2) and (4.3), the limit of ξ when $\beta \rightarrow \infty$ is:

$$\begin{aligned} \xi &= z\Phi(k) = z\Phi(-\Phi^{-1}(1-\lambda)) \\ &= z(1 - \Phi(\Phi^{-1}(1-\lambda))) \\ &= z\lambda \end{aligned} \tag{5.1}$$

Since $\psi = \xi$ in the limit, the critical state ψ is also given by $z\lambda$. For large z , the efficiency loss is sizeable. Nor is there any reason to suppose that this efficiency loss is smaller than in typical cases with positive noise. In fact, figure 4 suggests that the effect can be perverse, depending on the parameter values. Indeed, for

the more plausible case where y lies to the right on λz , an increase in β “flattens” the failure schedule, pushing up the failure point. Thus, more information leads to a greater incidence of coordination failure.

However, one consequence of an infinite β is the fact that the critical state ψ no longer depends on the prior mean y , so that the “coordination effect” of value at risk disappears. At face value, this is quite natural, since as β becomes large, the information content of the private signal swamps the information contained in the prior distribution. We say “at face value”, as such reasoning can be quite treacherous. Indeed, we will see one instance of this in our second formulation of transparency.

5.2. Case of Precise Private and Public Information

One element emphasized by those advocating greater “transparency” in financial markets is the timely provision of official statistics and other market related information in a public forum. Timely provision has to do with frequent and up to date data for public scrutiny. The goal of such dissemination would be to increase the precision α of the ex ante distribution, so as to reduce the overall uncertainty facing the market. However, since market participants will have access to other information in addition to such public information, we must regard the precision β of the private information as increasing at a faster rate. Here, we let both α and β tend to infinity, but keep the ratio $\alpha/\sqrt{\beta}$ constant - where the constant is small enough to guarantee uniqueness of equilibrium. Thus, suppose that for constant c ,

$$\alpha \rightarrow \infty, \quad \beta \rightarrow \infty, \quad \text{but} \quad \frac{\alpha}{\sqrt{\beta}} = c \leq \frac{\sqrt{2\pi}}{z}$$

Then, $\sqrt{\beta/(\alpha + \beta)} = 1/\sqrt{1 + c/\sqrt{\beta}} \rightarrow 1$, so that the limit of ψ is

$$\psi = z\Phi(c(\psi - y) + k) \tag{5.2}$$

Notice the re-appearance of the ex ante mean y in this expression. Even though the private signal swamps the public information, the ex ante mean is still relevant in determining the critical state ψ . Thus, the “coordination effect” in value at risk returns with a vengeance. Greater transparency in terms of better public (and private) information also has little obvious effect in promoting overall efficiency (compare (5.2) with (4.5)). At first, this is somewhat puzzling, since the information contained in the public signal ought to be dominated by the more accurate private signal. However, this is to neglect the information contained in

y concerning the beliefs of *other* creditors. The ex ante mean y is relevant not because of the information conveyed about the fundamentals, but rather because it conveys information about the distribution of other creditors' beliefs, and it is this which is crucial in strategic situations such as ours.

This last observation holds some important lessons for the conduct of public policy in dissemination of information. When calling for improved transparency, it is important to be clear as to *how* the improved information will improve the outcome. The mere provision of information will not be enough. However, if the improved information in one element of better coordination of the disparate market participants, the information may have some beneficial effect. This suggests that concrete institutional changes must accompany the provision of information if the information is to be effective.

In spite of the acknowledged simplicity of the model, we may nevertheless draw some lessons for the current debate concerning the reform of the international financial system. With the benefit of theoretical hindsight, it is perhaps not surprising that the provision of more information to market participants does not mitigate the problem. After all, we should draw a distinction between a single-person decision problem and a strategic situation. In a single-person decision problem, more information is always more valuable. When I debate whether to carry an umbrella into work, an accurate weather forecast will minimize both the inconvenience of carrying a bulky umbrella on a sunny day, and also the opposite inconvenience of getting caught in a shower without shelter. In such instances, "transparency" works.

However, it is far from clear whether better information will mitigate a coordination problem. There is little guidance from economic theory that better information about payoffs to players of a coordination game leads to greater incidence of successful coordination. Indeed, the intuition conveyed by existing theory is of a much more prosaic sort - typified by the debate on the Coase Theorem - in which all the emphasis is placed on the impediments to efficient bargaining. When the interested parties are diffuse and face uncertainty both about the fundamentals and the information of others, it would be overly optimistic to expect ex post efficient bargains to be struck.

We have already noted how instances of successful coordination by creditors - such as the bailout of Long Term Capital Management in September 1998 - have had a forceful facilitator organizing the bailout. In the case of LTCM, this role was played by the New York Fed. The U. S. Treasury has also played a key role in a number of episodes in recent years (Brazil in 1999, Korea in 1997/8). The

fact that these instances have involved U.S. institutions - and hence, instances where U.S. interests were important - is food for thought. Proponents of more elaborate multilateral institutions would do well to pause for thought on how the new institution will fare in the role of facilitator.

Appendix

In this appendix, we provide an argument for lemma 1. In fact, we can show a much stronger result - namely, that if there is a unique solution to $U(\xi) = \lambda$, then the switching strategy around ξ is not only the unique *equilibrium* strategy, it is also the only strategy which survives the iterated deletion of dominated strategies.

Consider first the expected payoff to rolling over the loan conditional on ξ when all others are using the switching strategy around some point $\hat{\xi}$. Denote this payoff as

$$u(\xi, \hat{\xi}) \tag{5.3}$$

This payoff is given by $1 - \Phi(\sqrt{\alpha + \beta}(\psi - \xi))$, where ψ is the failure point defined as the unique solution to the equation $\psi = z\Phi(\sqrt{\beta}(x(\hat{\xi}, y) - \psi))$. The conditional payoff $u(\xi, \hat{\xi})$ can be seen to satisfy the following three properties.

Monotonicity. u is strictly increasing in its first argument, and is strictly decreasing in its second argument.

Continuity. u is continuous.

Full Range. For any $\hat{\xi} \in \mathbb{R} \cup \{-\infty, \infty\}$, $u(\xi, \hat{\xi}) \rightarrow 0$ as $\xi \rightarrow -\infty$, and $u(\xi, \hat{\xi}) \rightarrow 1$ as $\xi \rightarrow \infty$.

By appealing to these features, we can define two sequences of real numbers. First, define the sequence

$$\underline{\xi}^1, \underline{\xi}^2, \dots, \underline{\xi}^k, \dots \tag{5.4}$$

as the solutions to the equations:

$$u(\underline{\xi}^1, -\infty) = \lambda$$

$$\begin{aligned}
u(\underline{\xi}^2, \underline{\xi}^1) &= \lambda \\
&\vdots \\
u(\underline{\xi}^{k+1}, \underline{\xi}^k) &= \lambda \\
&\vdots
\end{aligned}$$

In an analogous way, we define the sequence

$$\bar{\xi}^1, \bar{\xi}^2, \dots, \bar{\xi}^k, \dots \quad (5.5)$$

as the solutions to the equations:

$$\begin{aligned}
u(\bar{\xi}^1, \infty) &= \lambda \\
u(\bar{\xi}^2, \bar{\xi}^1) &= \lambda \\
&\vdots \\
u(\bar{\xi}^{k+1}, \bar{\xi}^k) &= \lambda \\
&\vdots
\end{aligned}$$

We can then prove:

Lemma A1. Let ξ solve $U(\xi) = \lambda$. Then

$$\underline{\xi}^1 < \underline{\xi}^2 < \dots < \underline{\xi}^k < \dots < \xi \quad (5.6)$$

$$\bar{\xi}^1 > \bar{\xi}^2 > \dots > \bar{\xi}^k > \dots > \xi \quad (5.7)$$

Moreover, if $\underline{\xi}$ and $\bar{\xi}$ are, respectively, the smallest and largest solutions to $U(\xi) = \lambda$, then

$$\underline{\xi} = \lim_{k \rightarrow \infty} \underline{\xi}^k \quad \text{and} \quad \bar{\xi} = \lim_{k \rightarrow \infty} \bar{\xi}^k. \quad (5.8)$$

Proof. Since $u(\underline{\xi}^1, -\infty) = u(\underline{\xi}^2, \underline{\xi}^1) = \lambda$, monotonicity implies $\underline{\xi}^1 < \underline{\xi}^2$. Thus, suppose $\underline{\xi}^{k-1} < \underline{\xi}^k$. Since $u(\underline{\xi}^k, \underline{\xi}^{k-1}) = u(\underline{\xi}^{k+1}, \underline{\xi}^k) = \lambda$, monotonicity implies $\underline{\xi}^k < \underline{\xi}^{k+1}$. Finally, since $U(\xi) = u(\xi, \xi) = u(\underline{\xi}^{k+1}, \underline{\xi}^k)$, and $\underline{\xi}^k < \underline{\xi}^{k+1}$, monotonicity implies that $\underline{\xi}^k < \xi$. Thus, $\underline{\xi}^1 < \underline{\xi}^2 < \dots < \underline{\xi}^k < \dots < \xi$. An exactly analogous argument shows that $\bar{\xi}^1 > \bar{\xi}^2 > \dots > \bar{\xi}^k > \dots > \xi$.

Now, suppose $\underline{\xi}$ is the smallest solution to $u(\xi, \xi) = \lambda$. By (5.6) and the monotonicity of u , $\underline{\xi}$ is the smallest upper bound for the sequence $\{\underline{\xi}^k\}$. Since $\{\underline{\xi}^k\}$ is an increasing, bounded sequence, it converges to its smallest upper bound. Thus $\underline{\xi} = \lim_{k \rightarrow \infty} \underline{\xi}^k$. Analogously, if $\bar{\xi}$ is the largest solution to $u(\xi, \xi) = \lambda$, then (5.7) and monotonicity of u implies that $\bar{\xi} = \lim_{k \rightarrow \infty} \bar{\xi}^k$. This proves the lemma.

Lemma A2. If σ is a strategy which survives k rounds of iterated deletion of interim dominated strategies, then

$$\sigma(\xi) = \begin{cases} F & \text{if } \xi < \underline{\xi}^k \\ R & \text{if } \xi > \bar{\xi}^k \end{cases} \quad (5.9)$$

The argument is as follows. Let σ^{-i} be the strategy profile used by all players other than i , and denote by $\tilde{u}^i(\xi, \sigma^{-i})$ the payoff to i of rolling over the loan conditional on ξ when the others' strategy profile is given by σ^{-i} . The incidence of failure is minimized when everyone is rolling over the loan irrespective of the signal, and the incidence of failure is *maximized* when everyone is foreclosing on the loan irrespective of the signal. Thus, for any ξ and any σ^{-i} ,

$$u(\xi, \infty) \leq \tilde{u}^i(\xi, \sigma^{-i}) \leq u(\xi, -\infty) \quad (5.10)$$

From the definition of $\underline{\xi}^1$ and monotonicity,

$$\xi < \underline{\xi}^1 \implies \text{for any } \sigma^{-i}, \tilde{u}^i(\xi, \sigma^{-i}) \leq u(\xi, -\infty) < u(\underline{\xi}^1, -\infty) = \lambda. \quad (5.11)$$

In other words, $\xi < \underline{\xi}^1$ implies that rolling over the loan is strictly dominated by foreclosing. Similarly, from the definition of $\bar{\xi}^1$ and monotonicity,

$$\xi > \bar{\xi}^1 \implies \text{for any } \sigma^{-i}, \tilde{u}^i(\xi, \sigma^{-i}) \geq u(\xi, \infty) > u(\bar{\xi}^1, \infty) = \lambda. \quad (5.12)$$

In other words, $\xi > \bar{\xi}^1$ implies that foreclosing on the loan is strictly dominated by rolling over. Thus, if strategy σ^i survives the initial round of deletion of dominated strategies,

$$\sigma^i(\xi) = \begin{cases} F & \text{if } \xi < \underline{\xi}^1 \\ R & \text{if } \xi > \bar{\xi}^1 \end{cases} \quad (5.13)$$

so that (5.9) holds for $k = 1$.

For the inductive step, suppose that (5.9) holds for k , and denote by U^k the set of strategies which satisfy (5.9) for k . We must now show that, if player i faces a strategy profile consisting of those drawn from U^k , then any strategy which is not in U^{k+1} is dominated. Thus, suppose that player i believes that he faces a strategy profile σ^{-i} consisting of strategies from U^k . Given this, the incidence of failure is minimized when σ^{-i} is the (constant) profile consisting of the $\bar{\xi}^k$ -trigger strategy, and the incidence of failure is *maximized* when σ^{-i} is the (constant) profile consisting of $\underline{\xi}^k$ -trigger strategy. Thus, for any ξ and any strategy profile σ^{-i} consisting of those from U^k ,

$$u(\xi, \bar{\xi}^k) \leq \tilde{u}^i(\xi, \sigma^{-i}) \leq u(\xi, \underline{\xi}^k) \quad (5.14)$$

From the definition of $\underline{\xi}^k$ and monotonicity, we have the following implication for any strategy profile σ^{-i} drawn from U^k .

$$\xi < \underline{\xi}^{k+1} \implies \tilde{u}^i(\xi, \sigma^{-i}) \leq u(\xi, \underline{\xi}^k) < u(\underline{\xi}^{k+1}, \underline{\xi}^k) = \lambda. \quad (5.15)$$

In other words, when $\xi < \underline{\xi}^k$ and when all others are using strategies from U^k , rolling over the loan is strictly dominated by foreclosing. Similarly, from the definition of $\bar{\xi}^k$ and monotonicity, we have the following implication for any strategy profile σ^{-i} consisting of those from U^k .

$$\xi > \bar{\xi}^{k+1} \implies \tilde{u}^i(\xi, \sigma^{-i}) \geq u(\xi, \bar{\xi}^k) > u(\bar{\xi}^{k+1}, \bar{\xi}^k) = \lambda. \quad (5.16)$$

In other words, when $\xi > \bar{\xi}^{k+1}$ and all others are using strategies from U^k , foreclosing on the loan is strictly dominated by rolling over. Thus, if strategy σ^i survives $k+1$ rounds of iterated deletion of dominated strategies,

$$\sigma^i(\xi) = \begin{cases} F & \text{if } \xi < \underline{\xi}^{k+1} \\ R & \text{if } \xi > \bar{\xi}^{k+1} \end{cases} \quad (5.17)$$

This proves the lemma.

With these preliminary results, we can complete the proof of Lemma 1. First, let us show that if ξ solves $U(\xi) = \lambda$, then there is an equilibrium in trigger strategies around ξ . Since $U(\xi) = u(\xi, \xi) = \lambda$, if everyone else is using the ξ -trigger strategy, the payoff to rolling over conditional on ξ is the same as that for foreclosing. Since u is strictly increasing in its first argument,

$$\xi_* < \xi < \xi^* \iff u(\xi_*, \xi) < \lambda < u(\xi^*, \xi)$$

so that the ξ -trigger strategy is the strict best reply.

Finally, let us show that if ξ is the unique solution to $U(\xi) = \lambda$, then there is no other equilibrium. From Lemma A1, we know that

$$\xi = \lim_{k \rightarrow \infty} \underline{\xi}^k = \lim_{k \rightarrow \infty} \bar{\xi}^k \quad (5.18)$$

so that the only strategy which survives the iterated deletion of dominated strategies is the ξ -trigger strategy. Among other things, this implies that the equilibrium in ξ -trigger strategies is the unique equilibrium.

The basic properties of our model conform to the class of supermodular games examined by Milgrom and Roberts (1990), in that the payoffs exhibit strategic complementarities, and the strategy set can be seen as a lattice for the appropriate ordering of strategies. The following features of our model echo the general results obtained by Milgrom and Roberts.

- There is a “smallest” and “largest” equilibrium, corresponding to the smallest and largest solutions to the equation $U(\xi) = \lambda$.
- Any strategy other than those lying between the smallest and largest equilibrium strategies can be eliminated by iterated deletion of dominated strategies. Thus, if $\underline{\xi}$ and $\bar{\xi}$ are, respectively, the smallest and largest solutions to $U(\xi) = \lambda$, then rationalizability removes all indeterminacy in a player’s strategy except for the interval $[\underline{\xi}, \bar{\xi}]$.
- If there is a unique solution to $U(\xi) = \lambda$, then there is a unique equilibrium, and this is obtained as the uniquely rationalizable strategy.

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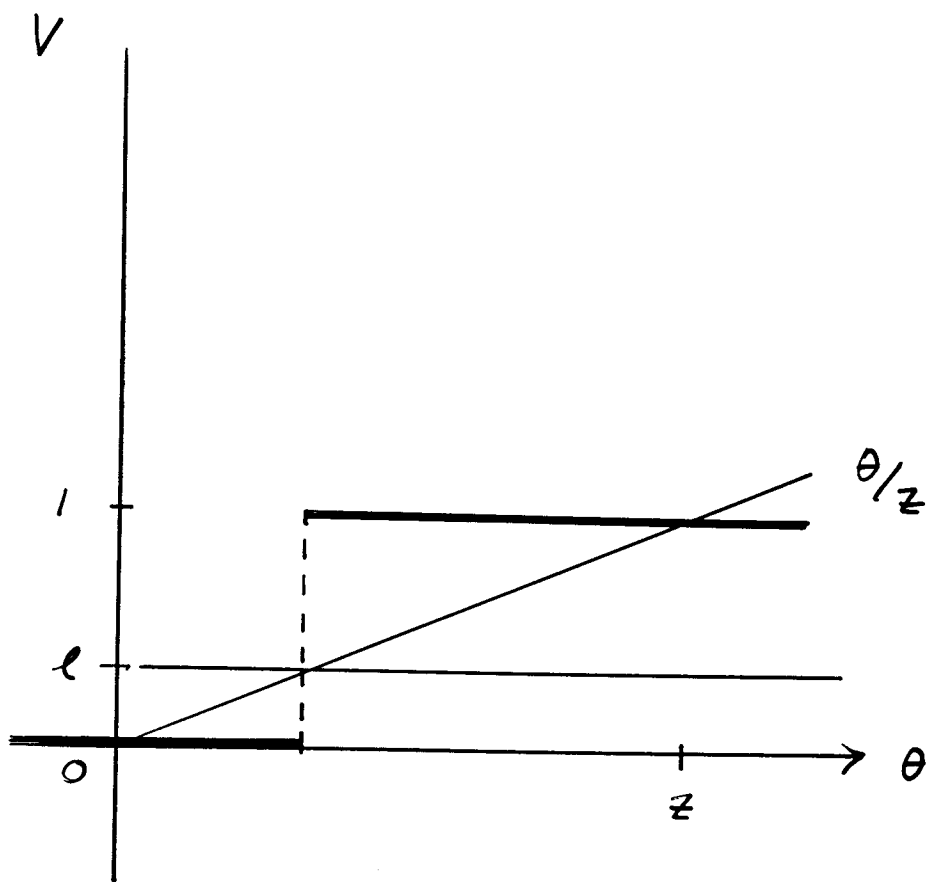


FIGURE 1

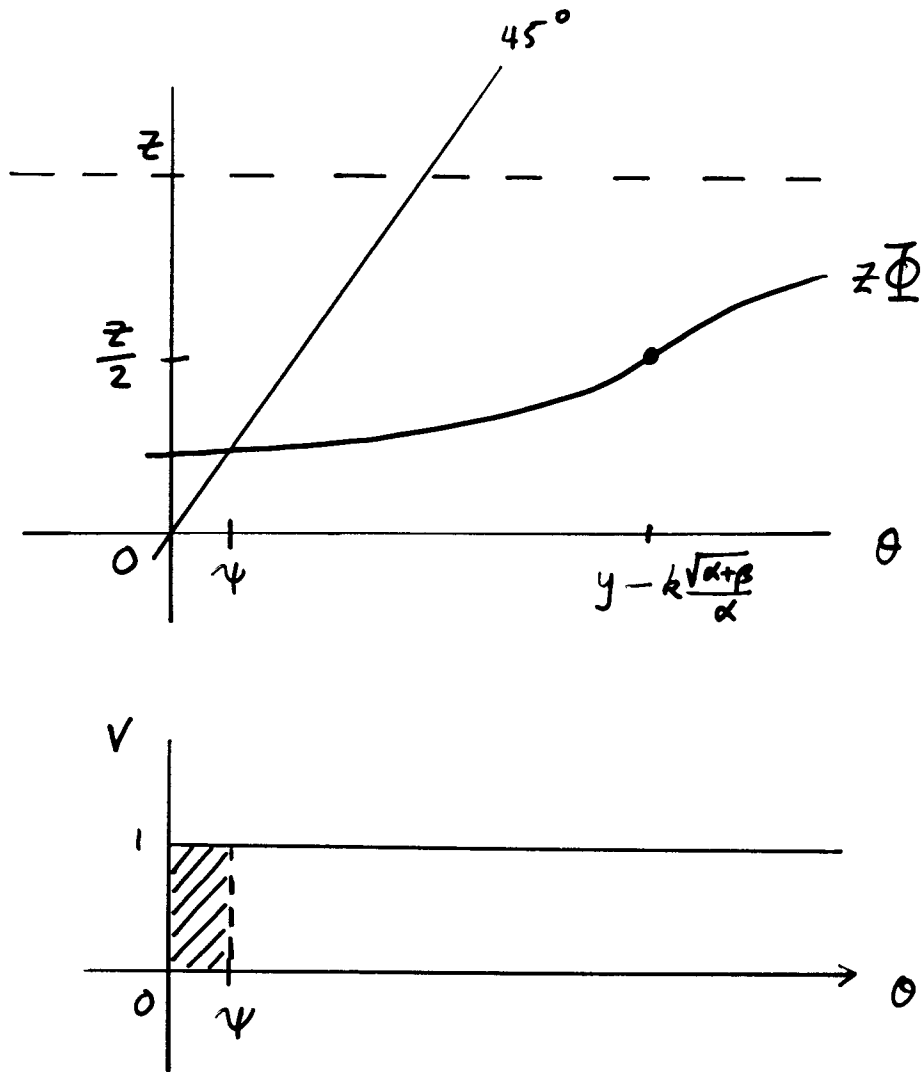


FIGURE 2

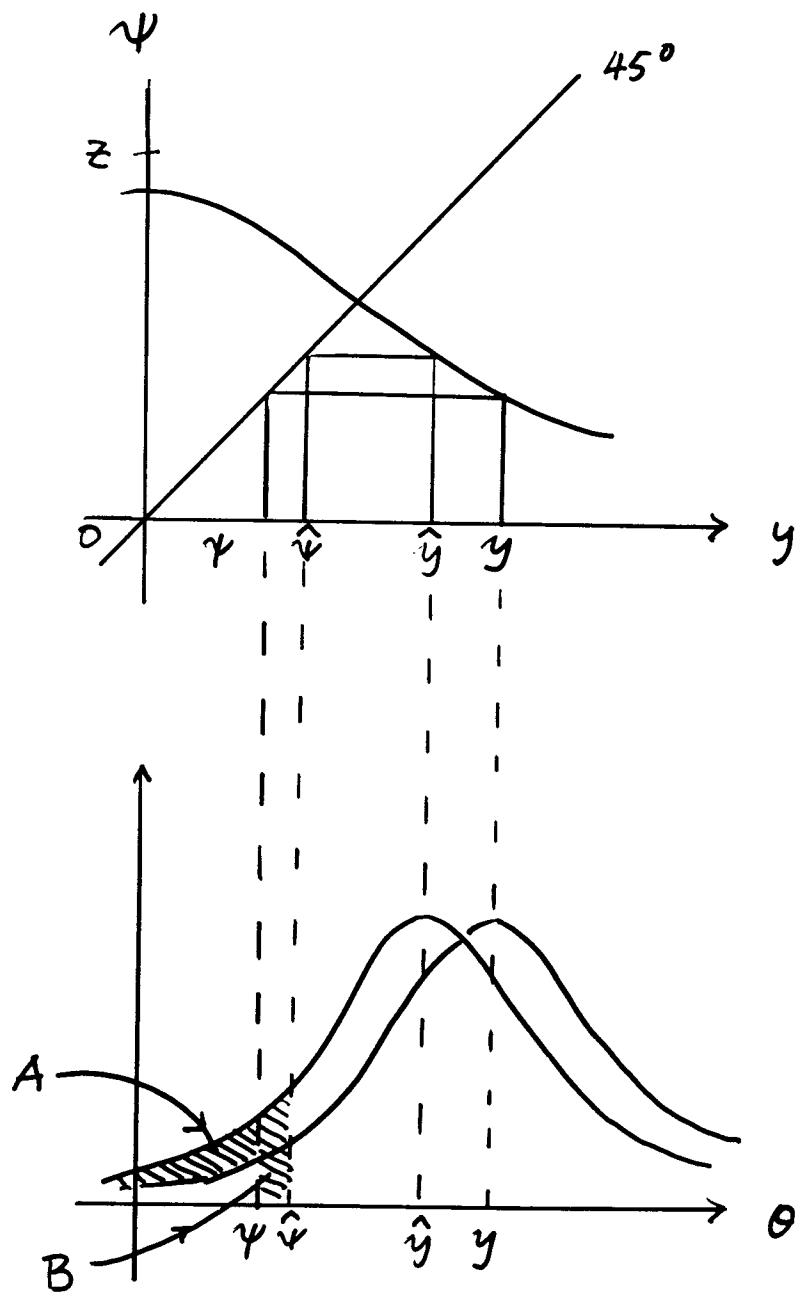
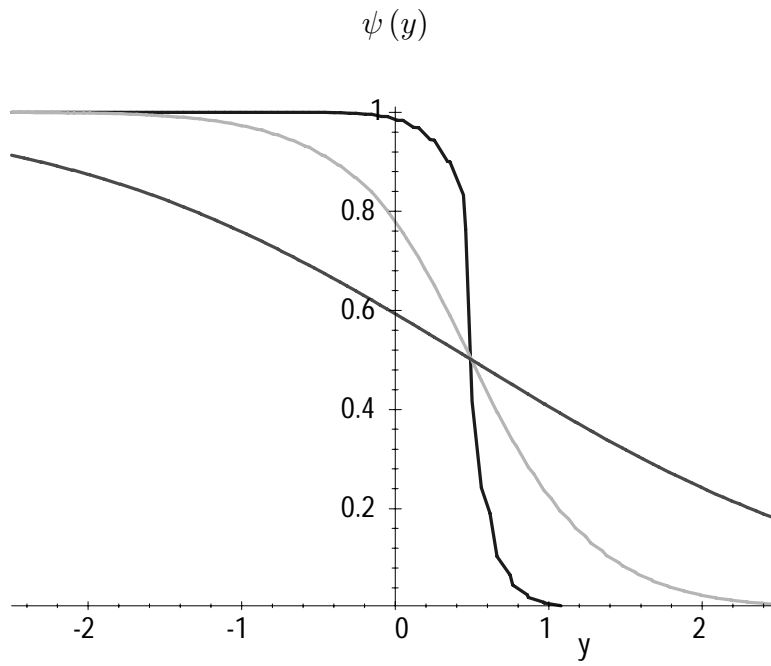


FIGURE 3



Plots of $\psi(y)$ when $\alpha/\sqrt{\beta}$ takes values 2.5, 1 and 0.4

[Figure 4]